

# Accretion in Protoplanetary Disks (conventional and transitional)

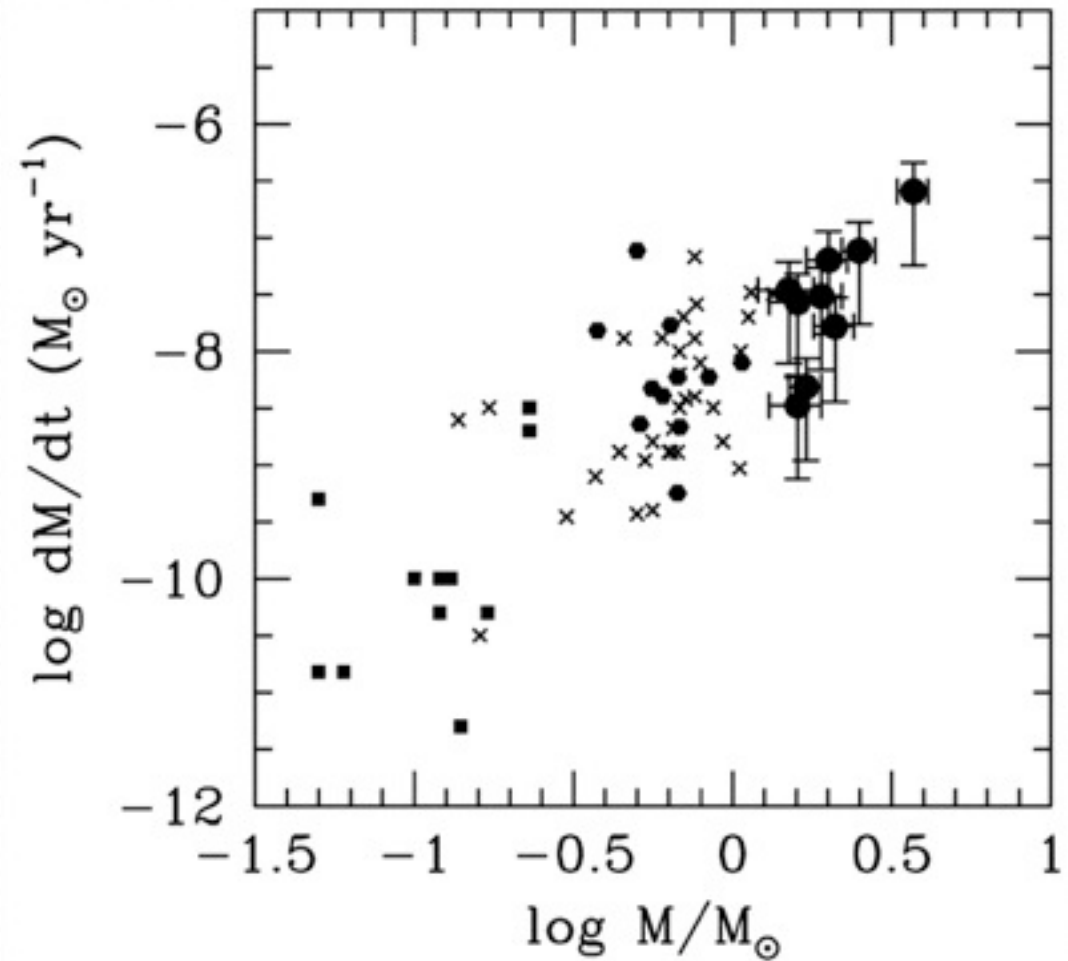
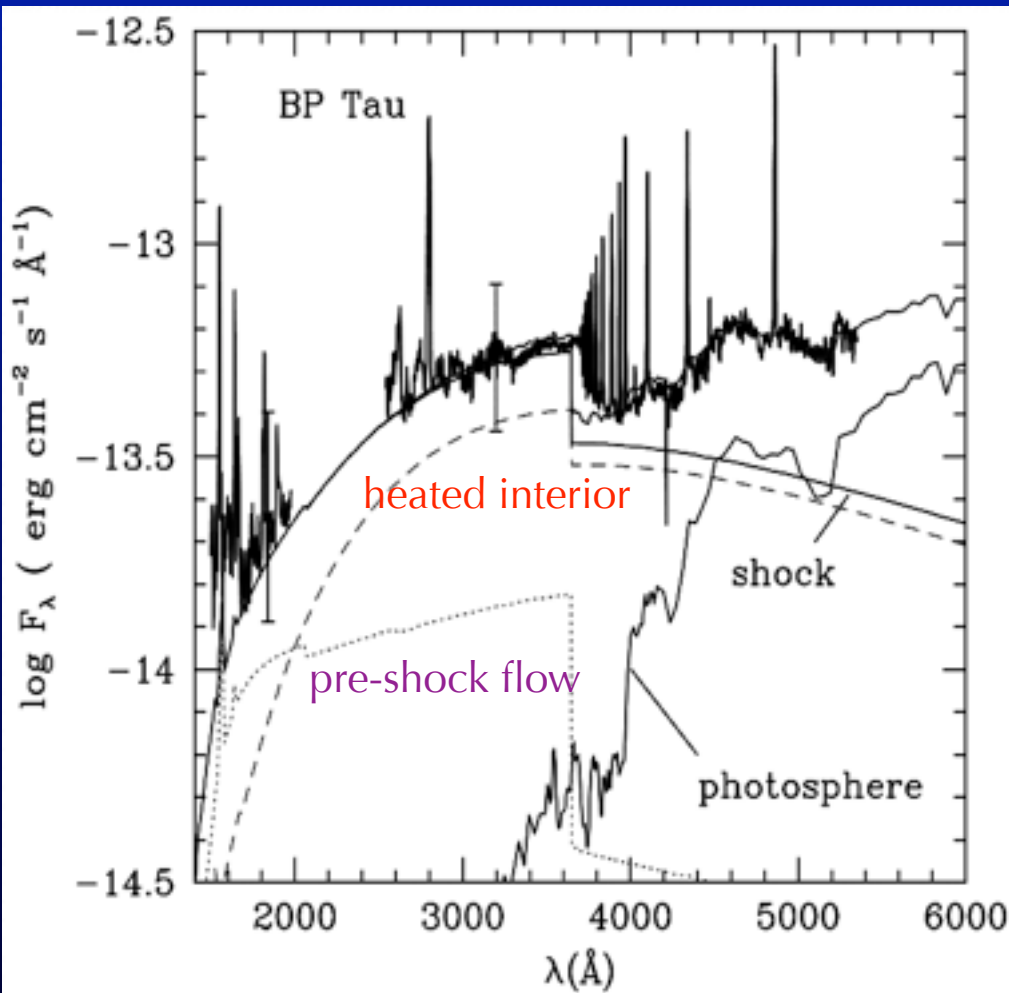
1000 AU

HH30



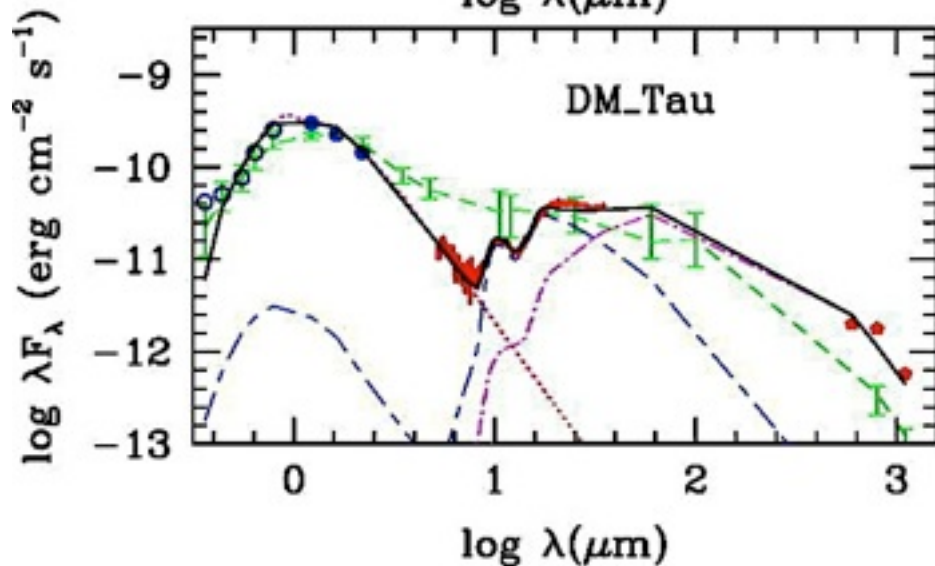
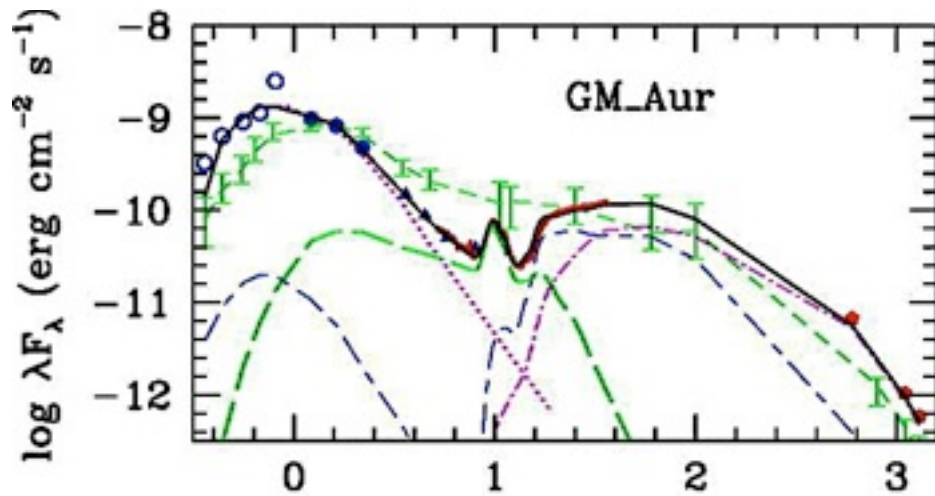
EC  
Daniel Perez-Becker  
(Berkeley)

# Pre-main-sequence stars accrete

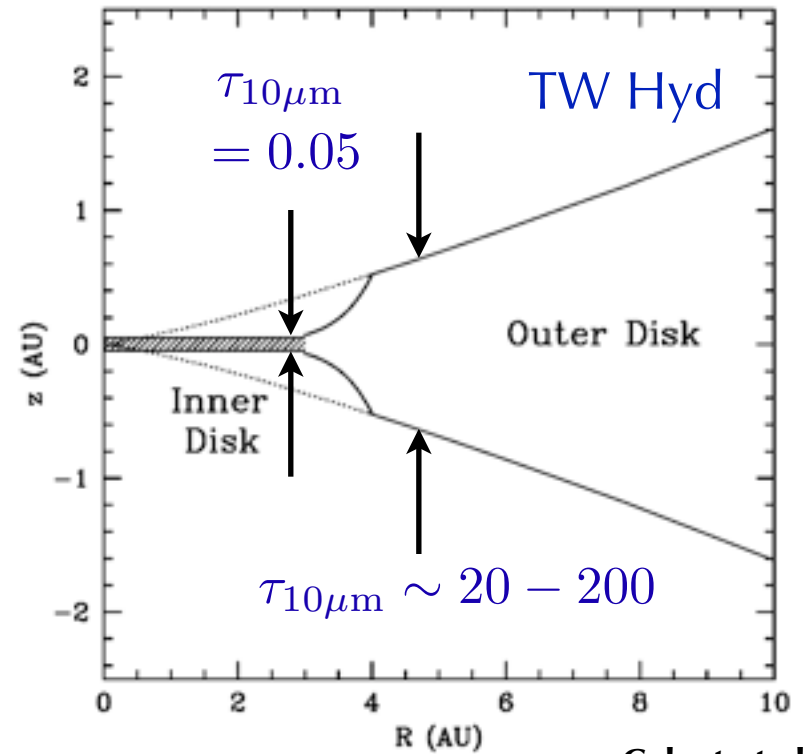


Blue excess powered by accretion

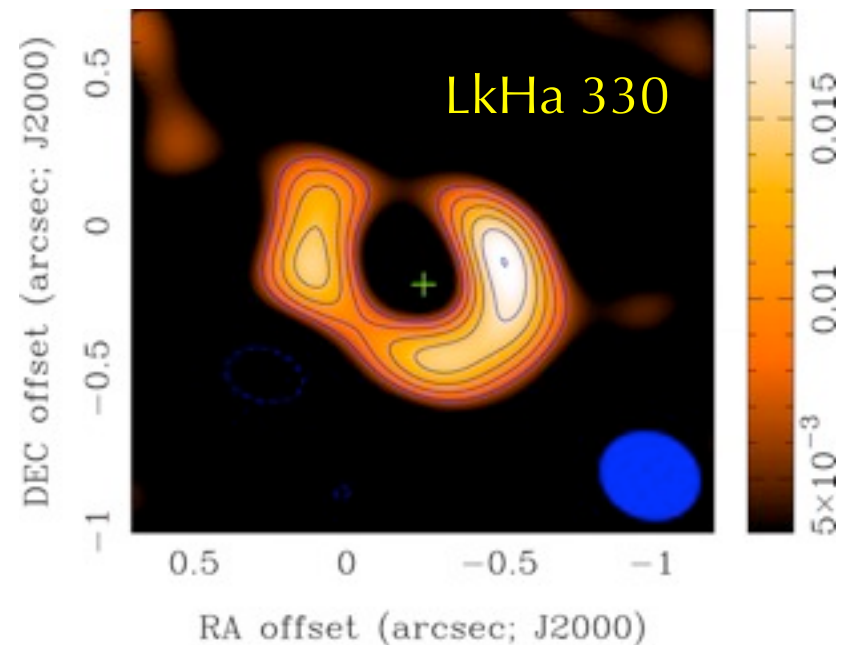
# Transitional Disks



Calvet et al. 05



Calvet et al. 02



Brown et al. 08

# Holes are not empty

- Mild near-IR excesses in some sources

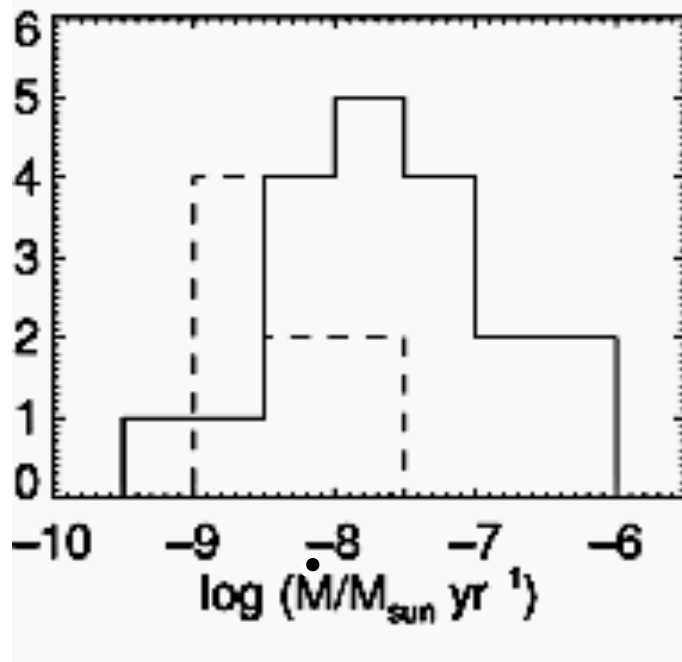
$$\tau_{10\mu\text{m}} \sim 0.002 - 0.05$$

- Many accrete

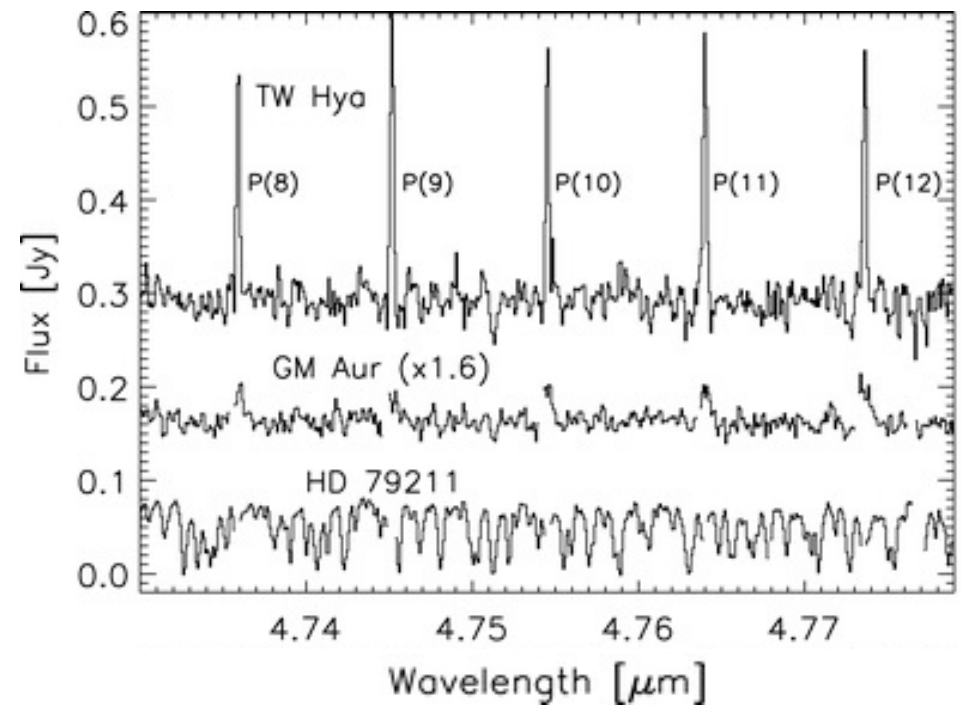
$$\dot{M} \sim 0.1 \times \text{median T Tauri}$$

- Inner molecular gas disks

$$\Sigma(\text{H}_2) > 0.1 \text{ g cm}^{-2} \text{ at } \sim 0.2\text{AU}$$



Najita et al. 07



Salyk et al. 07

Puzzle:  $1000 \times$  smaller  $\tau$  but comparable  $\dot{M}$

Theories:

- Grain growth
- Clearing by companion

Not mutually exclusive

# Clearing by companion (Transitional = Circumbinary)

Binary separation

$$a_{\text{binary}} \approx 8 \text{ AU}$$

$\approx$  Hole radius

$$a_{\text{rim}} \approx 10 \text{ AU}$$

$$\tau_{10\mu\text{m}} < 0.002$$

$$\dot{M}_* < 10^{-10} M_{\odot}/\text{yr}$$

No CO gas out to 2 AU

D'Alessio et al. 05

Najita et al. 07

Blake, Salyk, personal comm.

## CoKu Tau/4

Ireland & Kraus 08 (Keck AO)

Artymowicz & Lubow 94

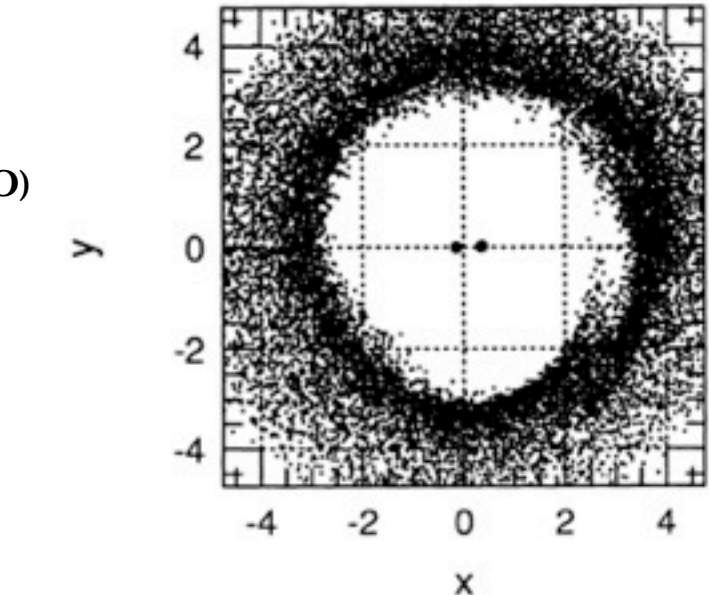
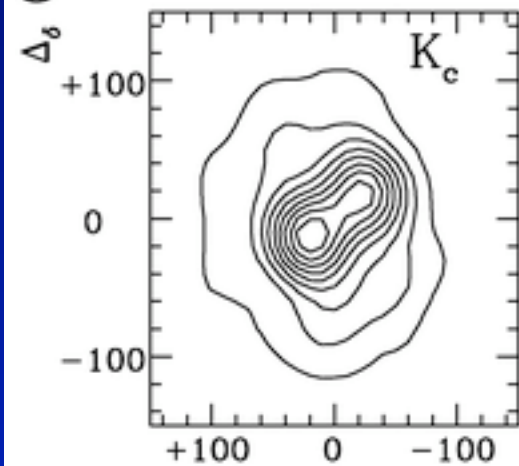
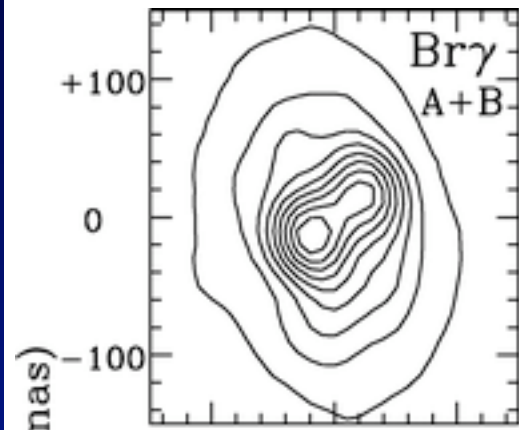
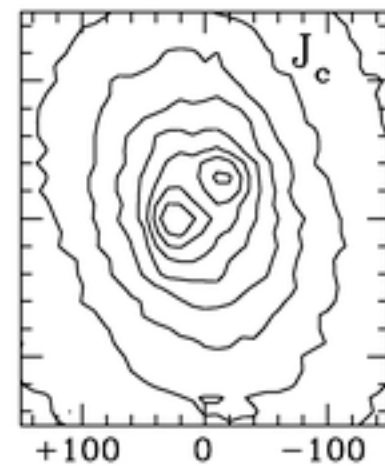
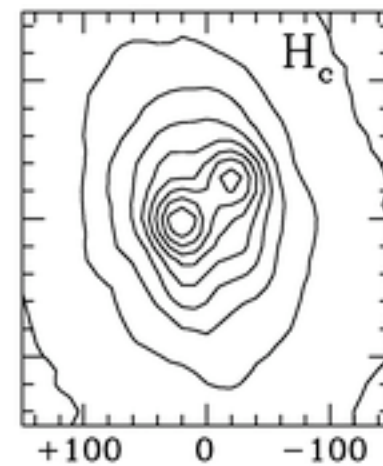
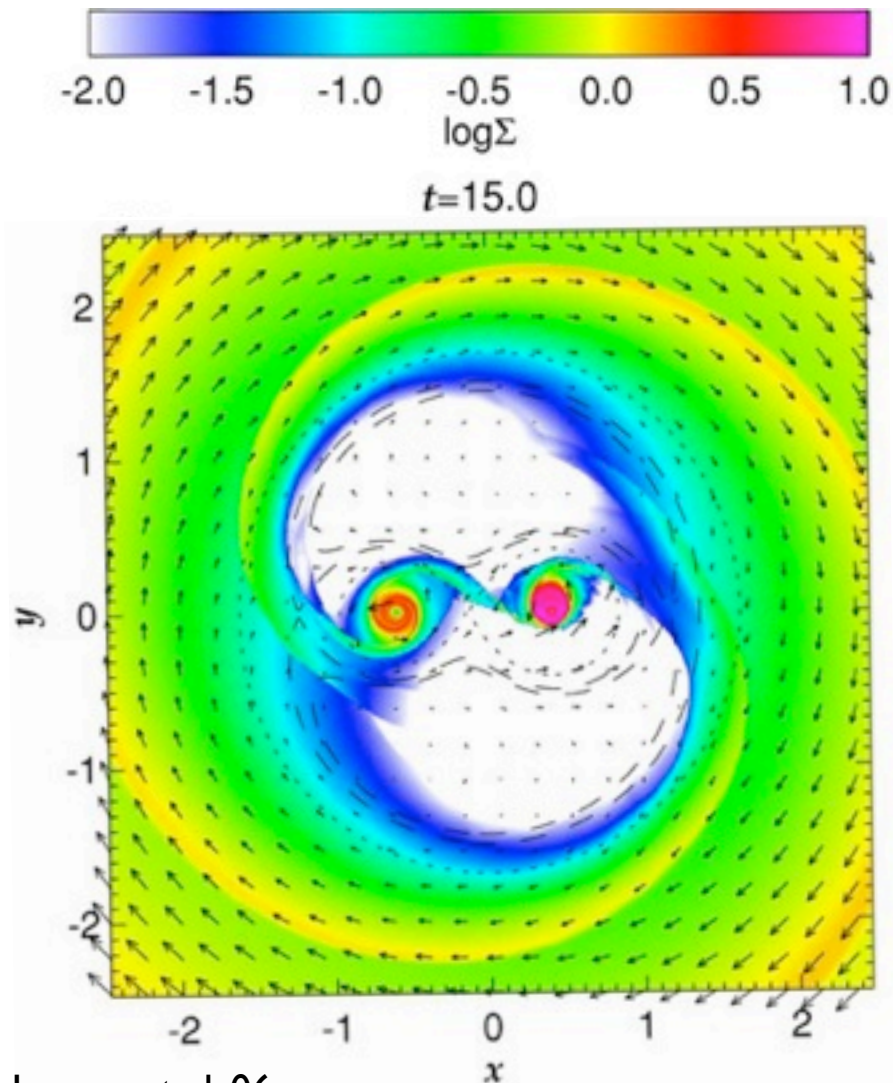


FIG. 10.—A gap out to  $r \approx 2.8a$  surrounding a  $\mu = 0.3$ ,  $e = 0.5$  binary. The gap is much larger than in Fig. 9, extending to between 4:1 and 5:1 orbital commensurabilities. Stars are at their 50th periastron passage.



$\Delta_{\alpha}$  (mas)

# Clearing by companion (Transitional = Circumbinary)



Hanawa et al. 06

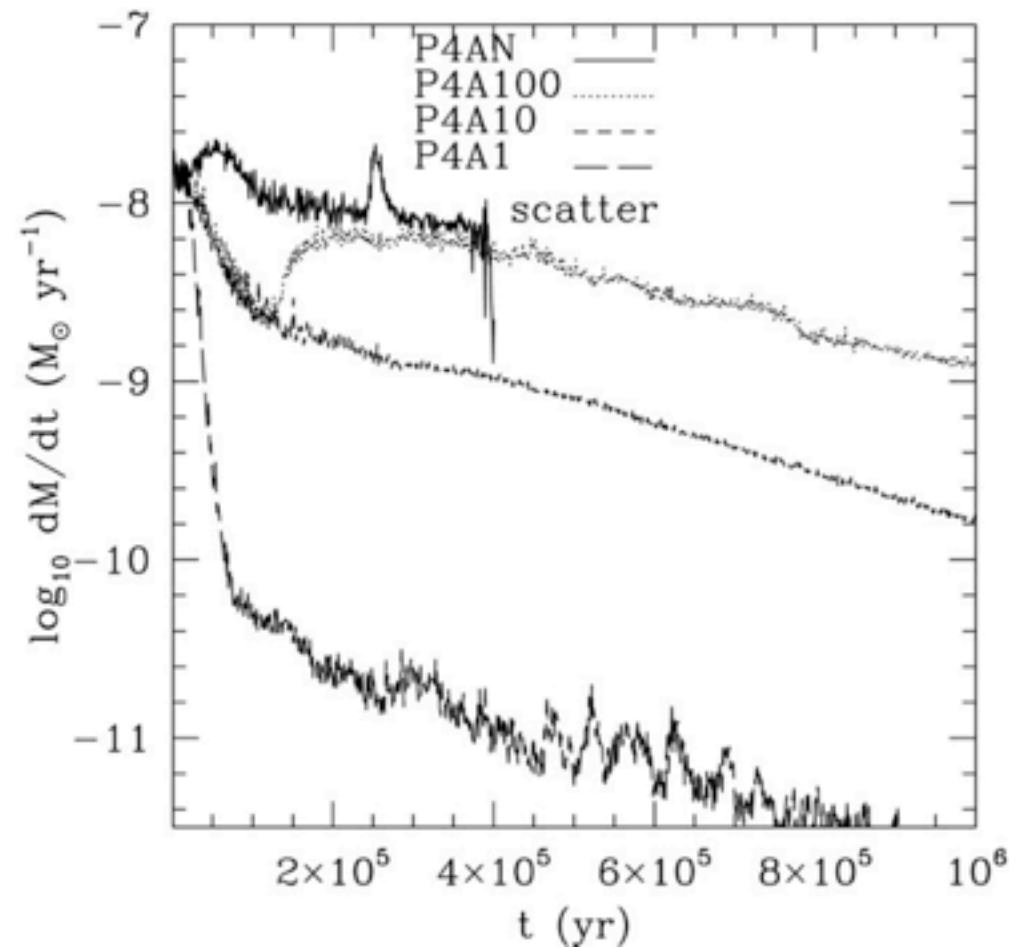
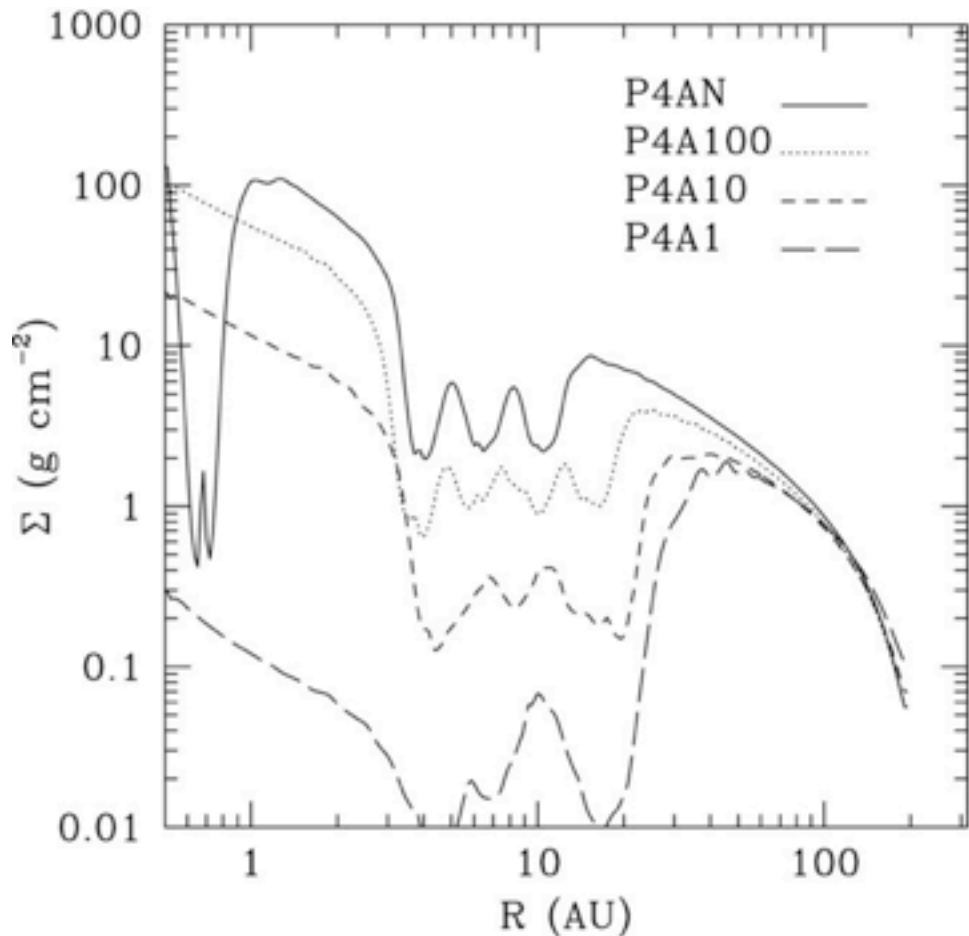
Mass can still accrete onto star  
(viscosity / pressure / eccentricity /  
mass ratio)

Fast flow (up to radial free-fall)  
implies low surface density

Resolves the puzzle of  
similar  $\dot{M}$  but  
1000x lower optical depth

# Clearing by multiple planets

Simulation of 4-planet system in viscous disk



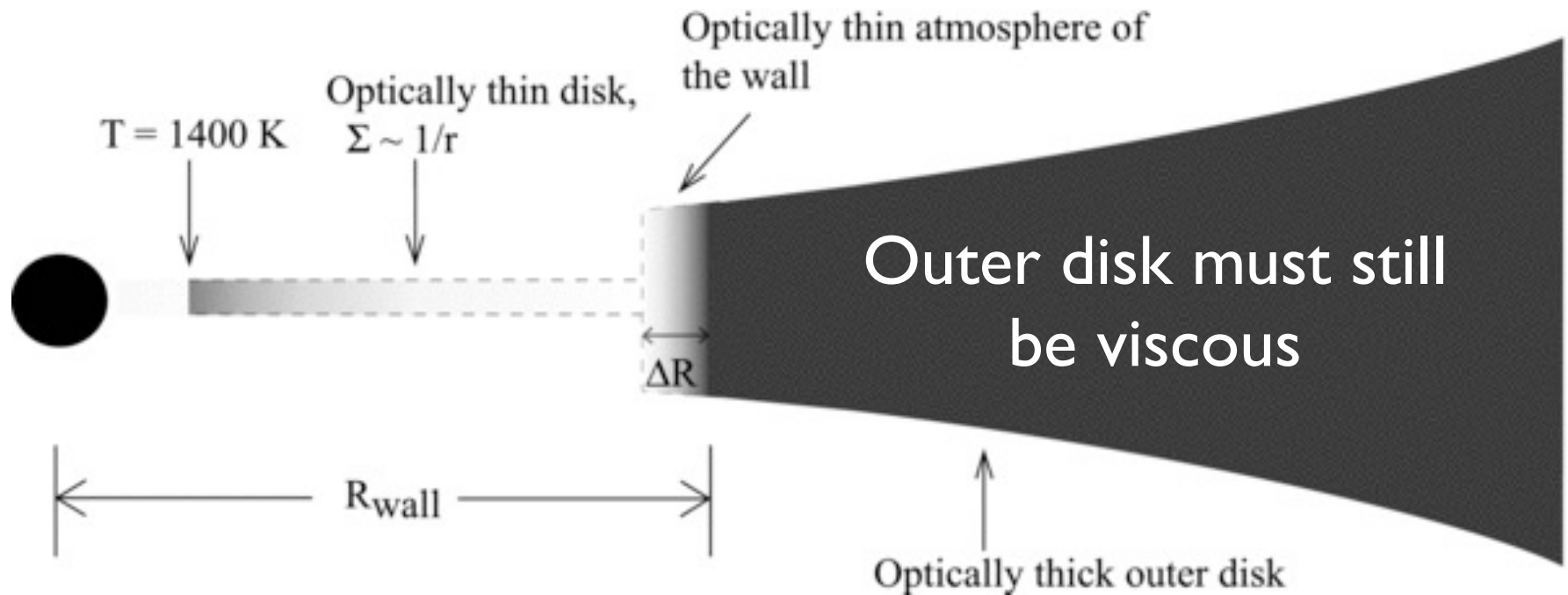
2D FARGO

Zhu et al. 11

Right sign, too small magnitude  
– unless dust is also depleted

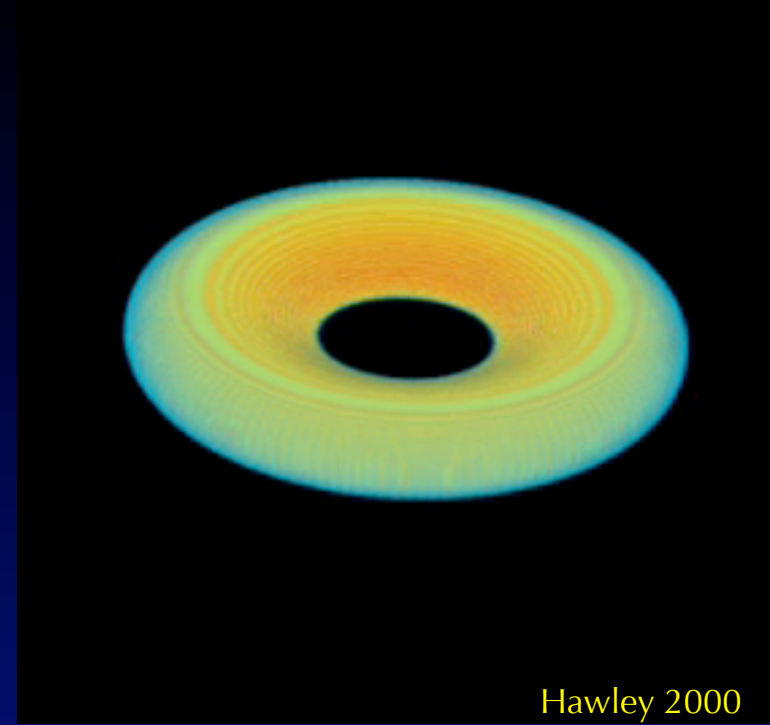


# Planets inside the hole do not explain disk accretion



# Disk accretion

Magneto-rotational instability (MRI)  
= linear instability  
which drives turbulence  
in weakly magnetized,  
outwardly shearing flows



Hawley 2000

## Requirements

1. Magnetic flux freezing  
(defeat Ohmic dissipation)

(Fleming, Stone, & Hawley 00)

$$\text{Re}_M \equiv \frac{c_s h}{\eta} \propto \frac{n_e}{n}$$

$$> \text{Re}_M^* \approx 10^2 - 10^4$$

2. Good neutral-ion coupling  
(defeat ambipolar diffusion)

(Blaes & Balbus 94;

Hawley & Stone 98; Bai & Stone 11)

$$\text{Am} \equiv \frac{n_i \langle \sigma v \rangle_{in}}{\Omega} > \text{Am}^* \approx 1-100$$

# Surface Layer Accretion by the MRI

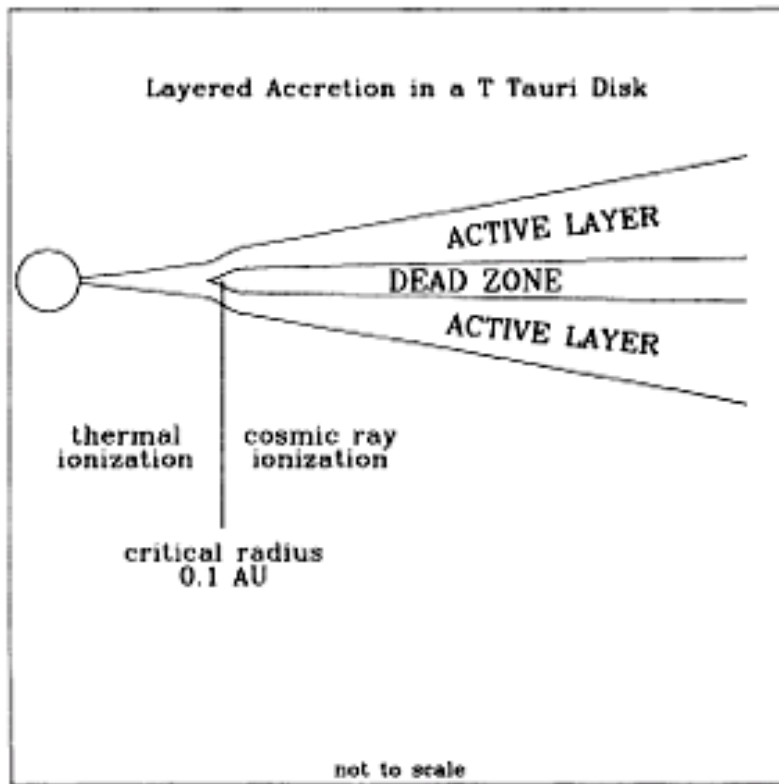
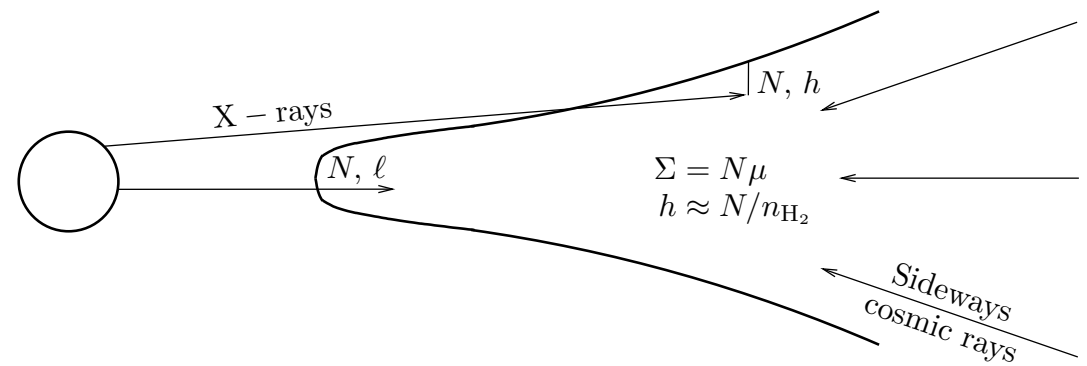


FIG. 1.—Sketch showing the key features of a layered accretion disk. Inside  $\approx 0.1$  AU, where  $T \approx 10^3$  K, collisional ionization is sufficient to couple the magnetic field to the gas. Outside this critical radius cosmic rays ionize a layer of thickness  $\approx 100 \text{ g cm}^{-2}$  on either side of the disk. Sandwiched between these active layers is a dead zone where no accretion occurs.

Gammie 96



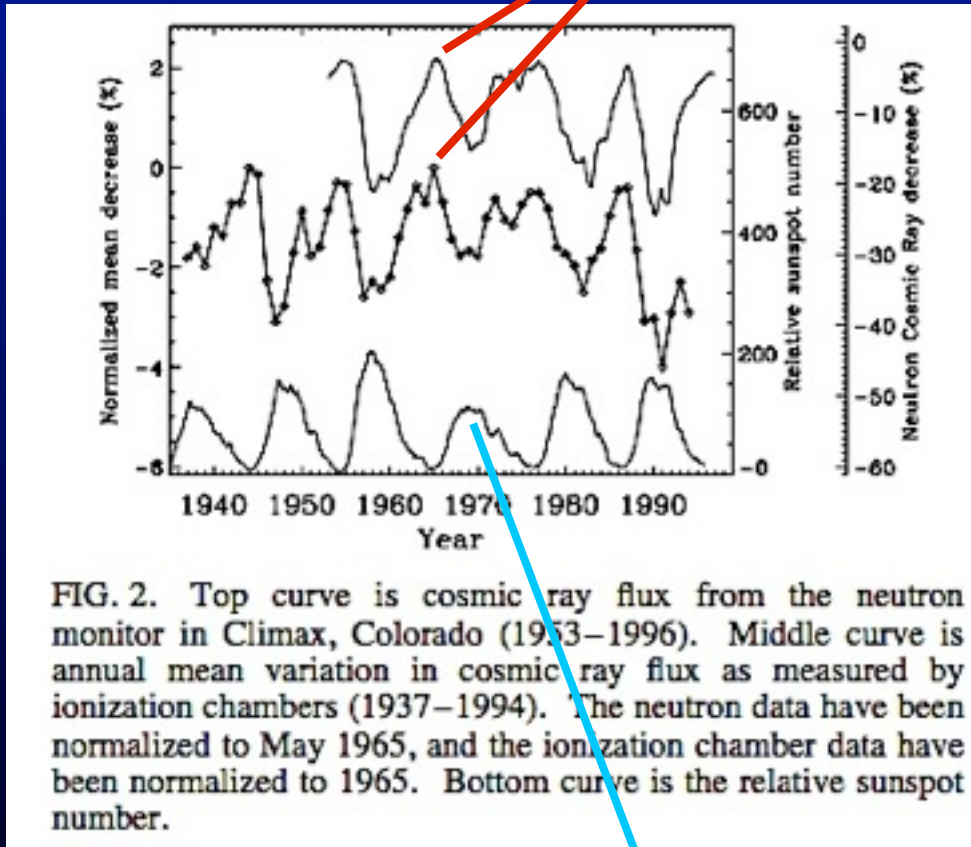
## Sources of ionization

1. Cosmic rays
2. Stellar X-rays
3. Stellar UV

Glassgold et al. 97  
 Sano et al. 00  
 Ilgner & Nelson 06  
 Bai & Goodman 09  
 Turner et al. 10  
 Perez-Becker & EC 11a  
 Perez-Becker & EC 11b

# Galactic cosmic rays blocked by stellar wind

cosmic ray flux



sunspot number

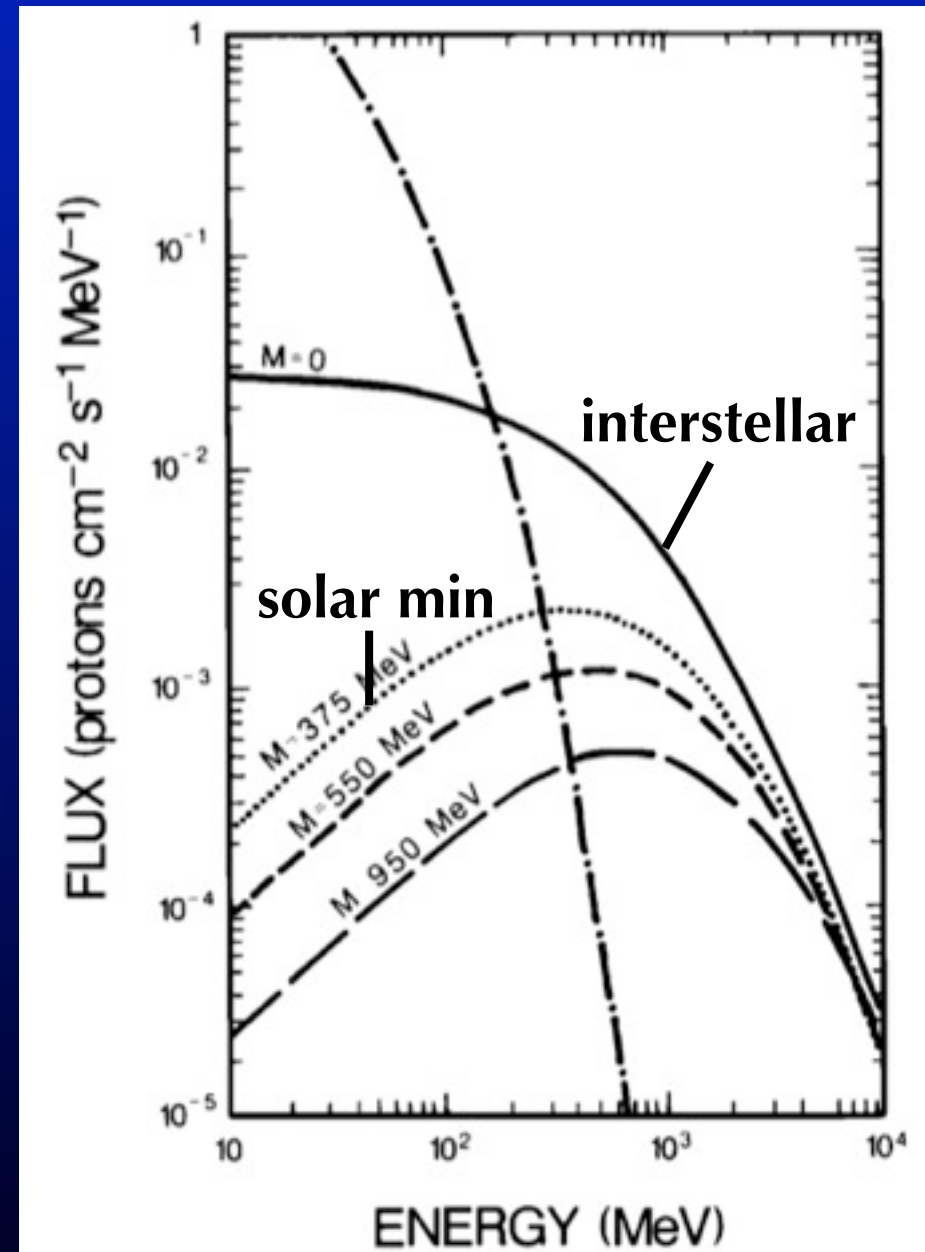
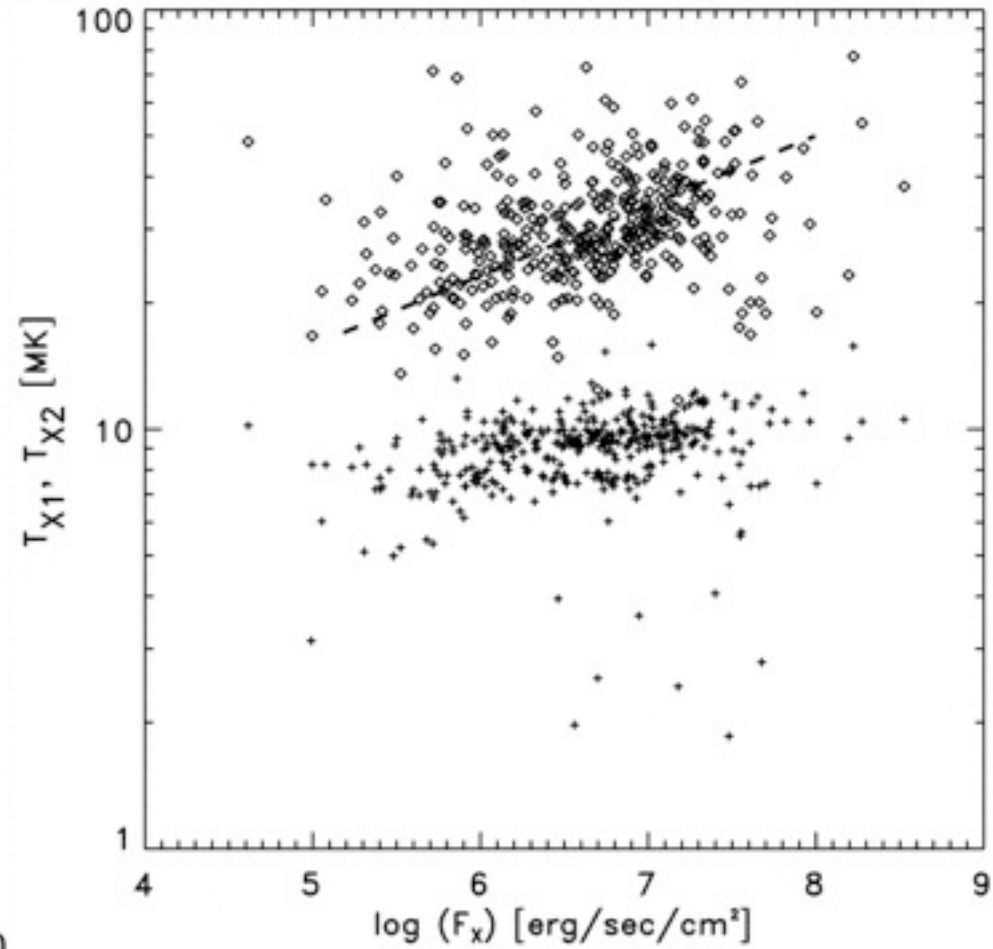
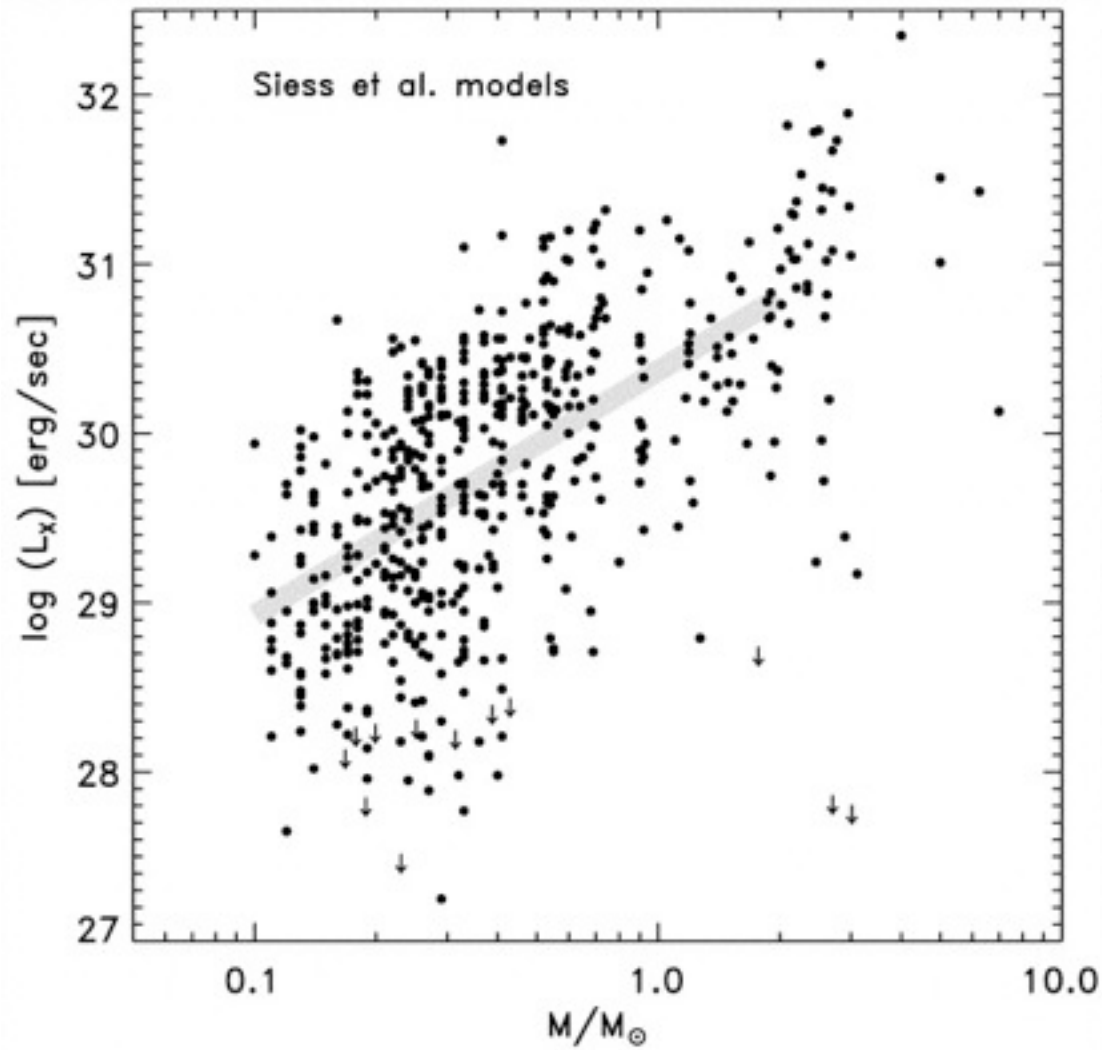
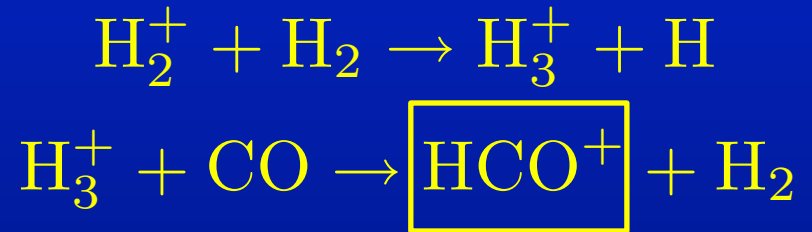
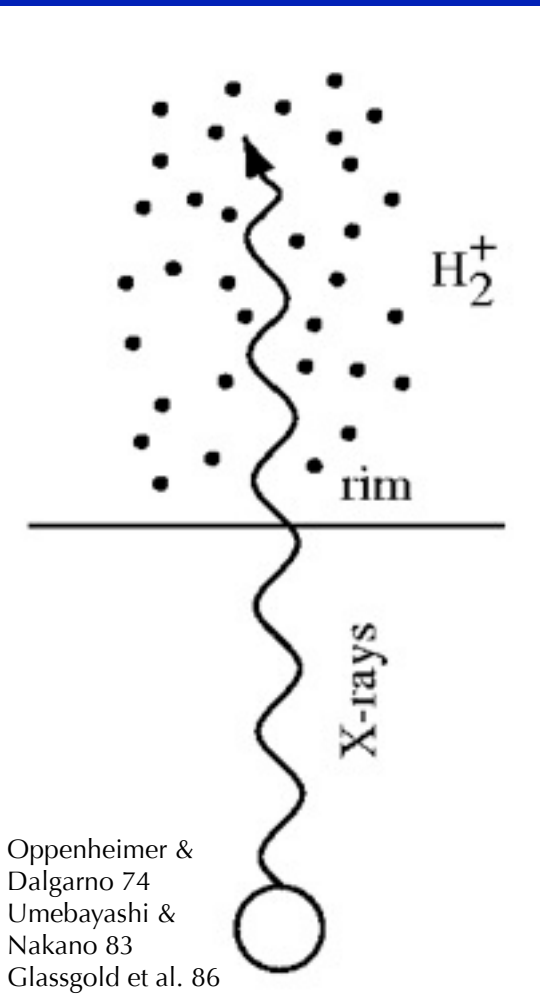


Fig. 1. The omnidirectional fluxes as a function of kinetic energy of solar protons with  $R_0 = 100$  MV (the dot-dashed line) and of GCR protons in the solar system (using equation (1)), for no modulation ( $M = 0$ ) and for three levels of modulation: solar maximum ( $M = 950$  MeV), the 11-year average ( $M = 550$  MeV), and solar minimum ( $M = 375$  MeV).

# Pre-main sequence stars are X-ray luminous





free  
metal  
Mg

charge  
transfer

$$\beta_t \sim 10^{-9} \text{ cm}^3 \text{ s}^{-1}$$



$e^-$

dissociative  
recombination

$$\beta_{\text{diss}} \sim 3 \times 10^{-7} \text{ cm}^3 \text{ s}^{-1}$$



$e^-$

radiative  
recombination

$$\beta_{\text{rec}} \sim 4 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$$



grain<sup>-</sup>

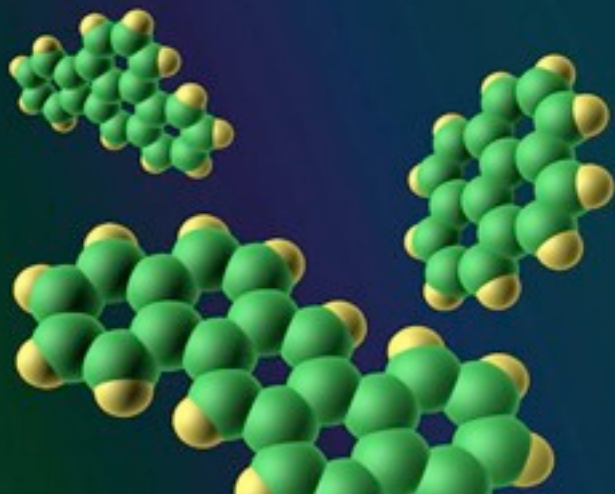
neutralization onto charged particles



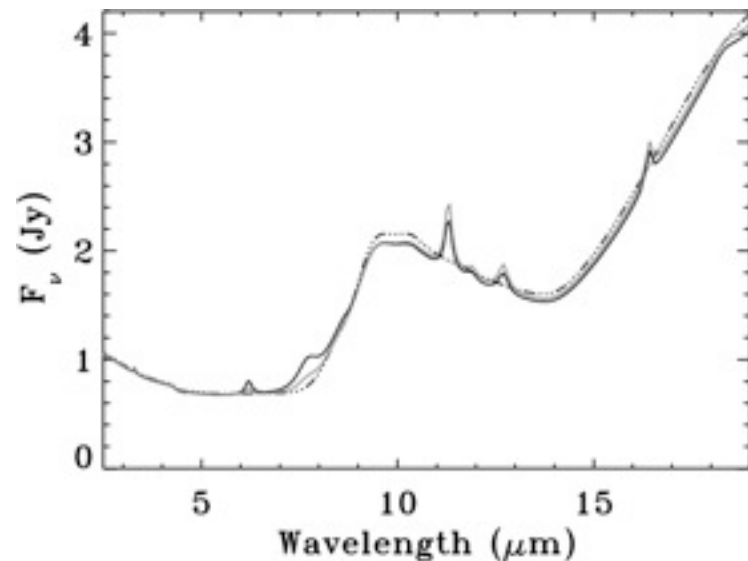
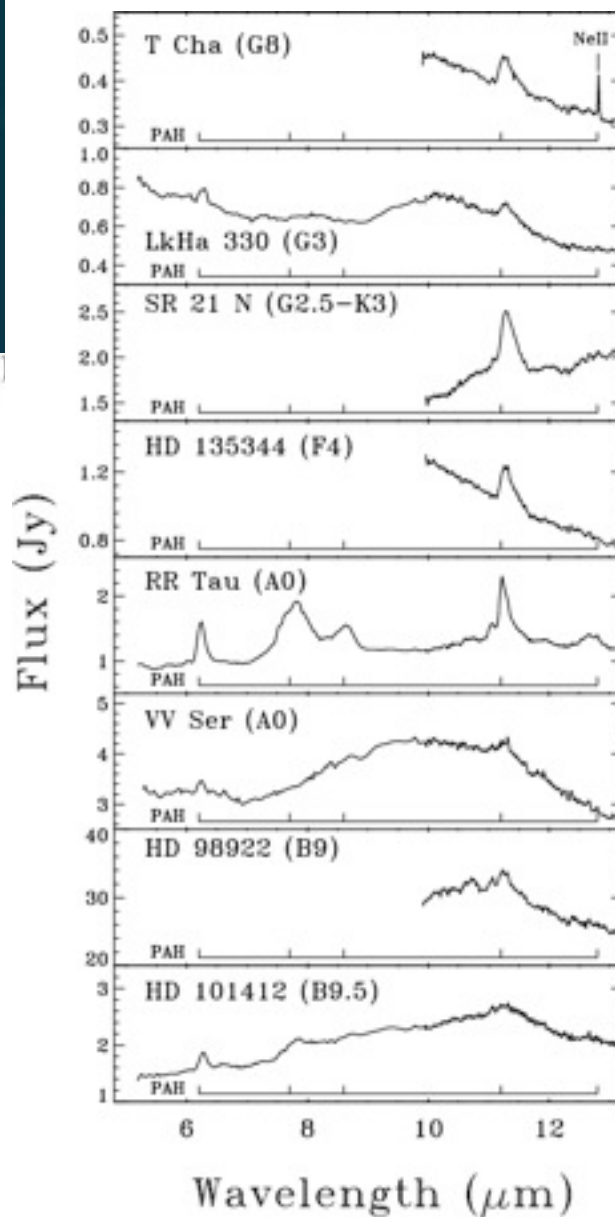
PAH<sup>-</sup>



# Polycyclic Aromatic Hydrocarbons (PAHs)



Formula	Name	Structure
$C_{20}H_{12}$	Benzo(j)fluoranthene	
	Benzo(k)fluoranthene	
	Benzo(e)pyrene	
	Perylene	
$C_{20}H_{14}$	9,10-Dihydrobenzo(e)pyrene	
$C_{22}H_{12}$	Benzo[ghi]perylene	
$C_{22}H_{14}$	Pentacene	
$C_{24}H_{12}$	Coronene	
$C_{42}H_{18}$	Hexabenzocoronene-A	

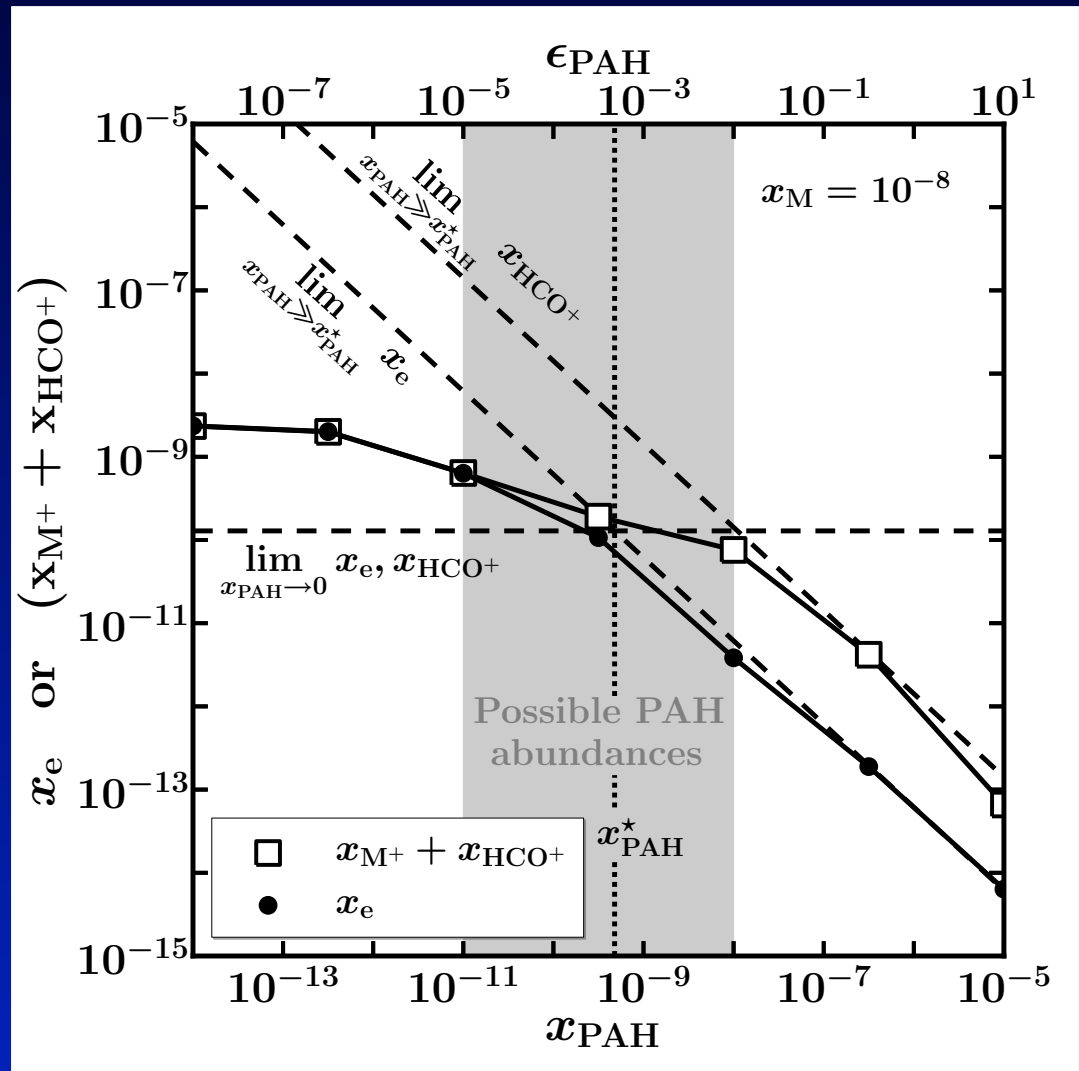
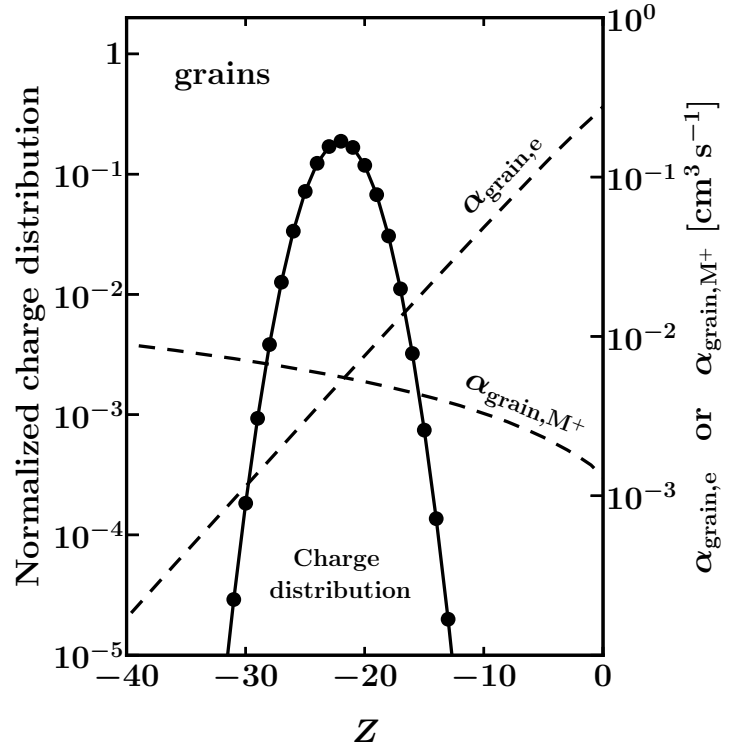
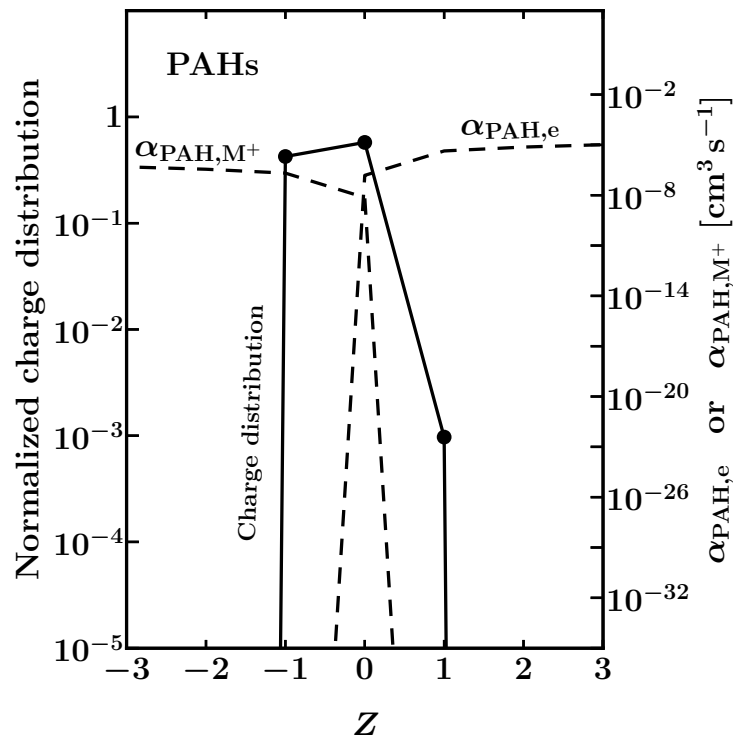


PAH abundance ~  
0.01-10 ppb H<sub>2</sub>  
  
(in diffuse ISM  
~1 ppm H)

Allamandola et al. 99  
Geers et al. 06

# Charge Balance

X-rays  $\Rightarrow$   $\text{HCO}^+$ ,  $\text{Mg}^+$   $\left\{ \begin{array}{l} e^- \\ \text{grain}^- (1 \mu\text{m}) \\ \text{PAH}^- (6 \text{ \AA}) \end{array} \right.$

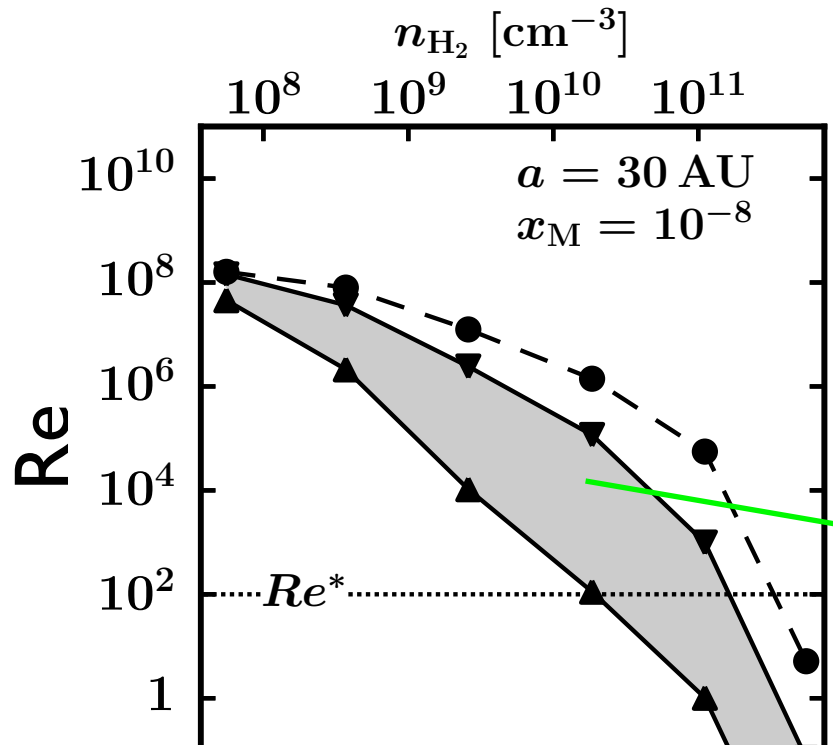




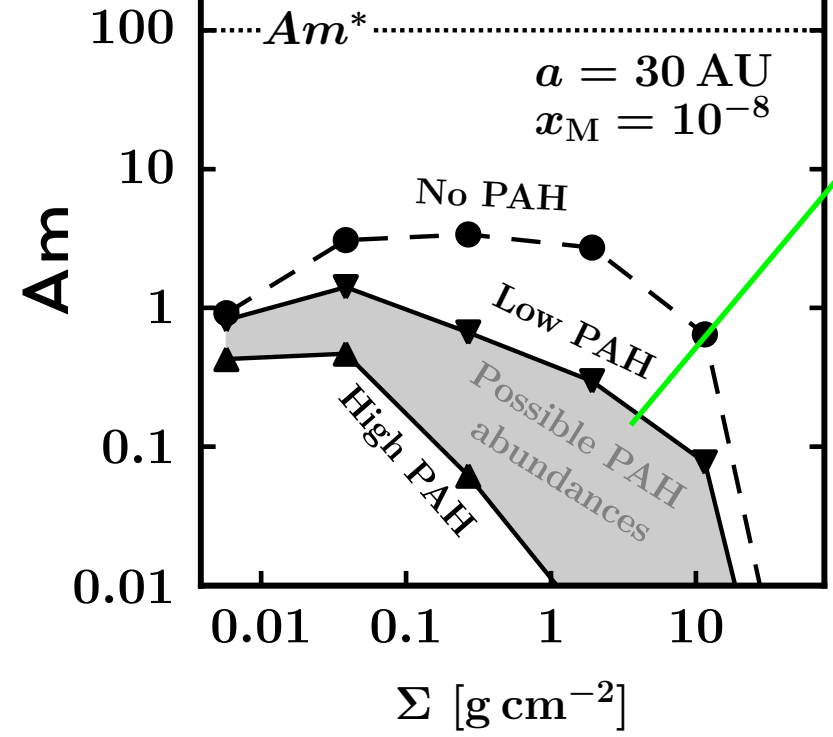
# X-ray ionization only

Field may be frozen to plasma ✓  
But ions decoupled from neutrals ✗

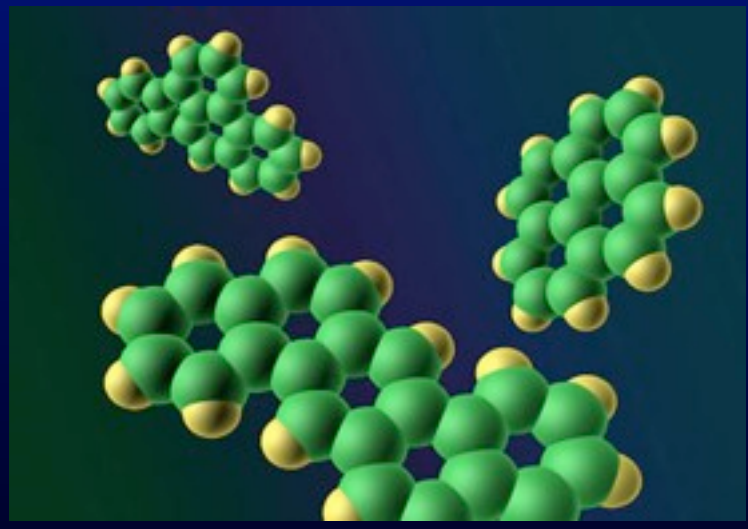
Ohmic dissipation



Ambipolar diffusion

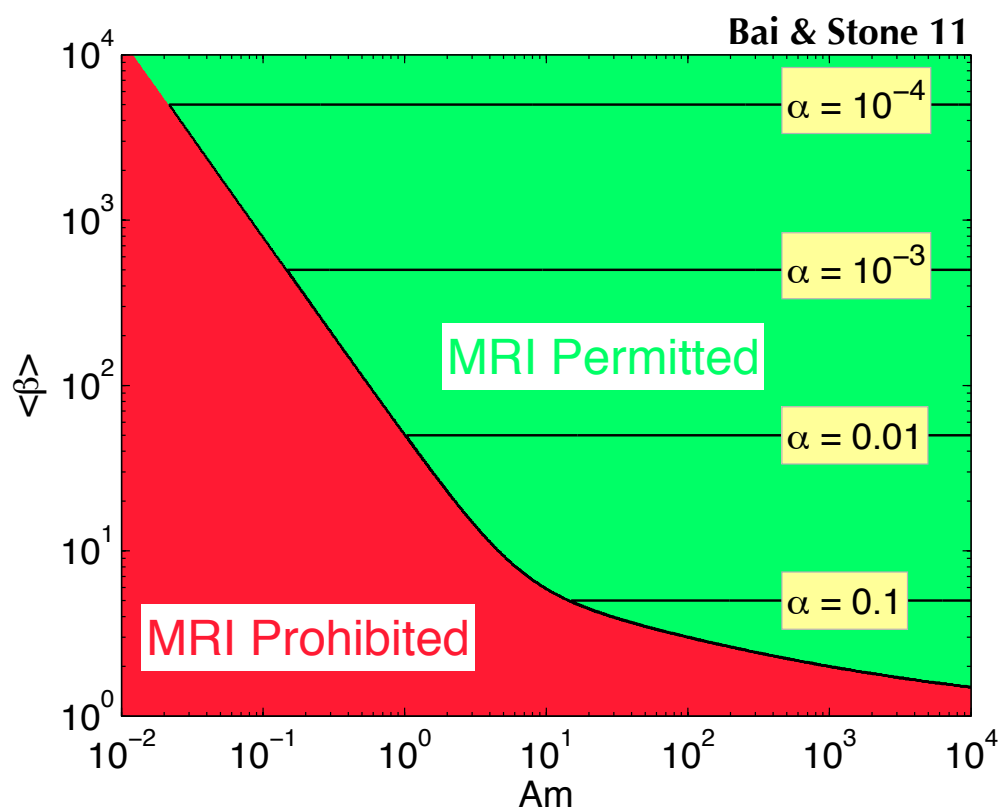


region allowed by PAHs



(0.01-10 ppb  $H_2$ )

# MRI with ambipolar diffusion



$$\alpha \approx 1/(2\beta)$$

and  $\beta_{\min}(A_m)$

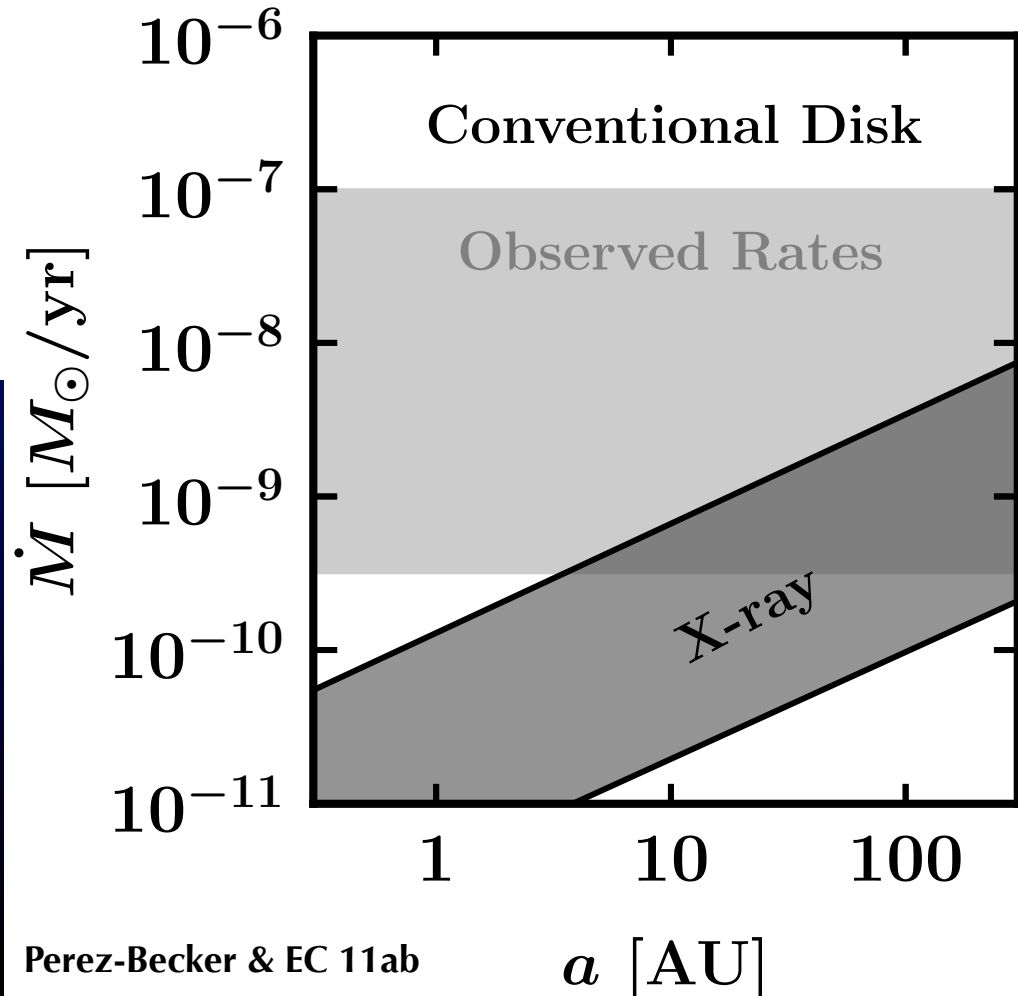
$$\Rightarrow \alpha_{\max}(A_m)$$

Kunz & Balbus 94  
 Hawley et al. 95  
 Desch 04  
 Pessah 10  
 Bai & Stone 11

$$\alpha_{\max}(A_m) \text{ and } A_m(\Sigma)$$

$$\Rightarrow \dot{M}$$

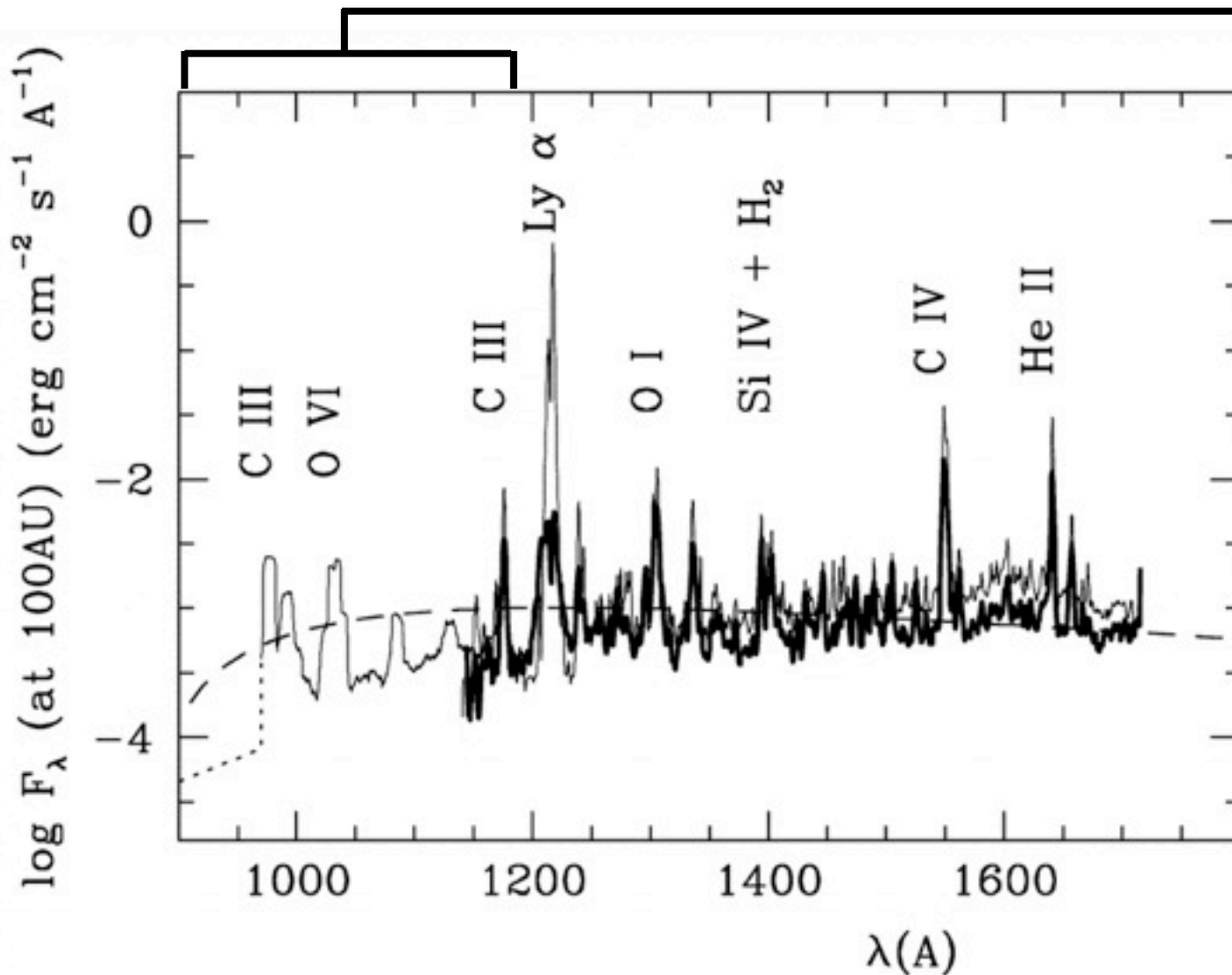
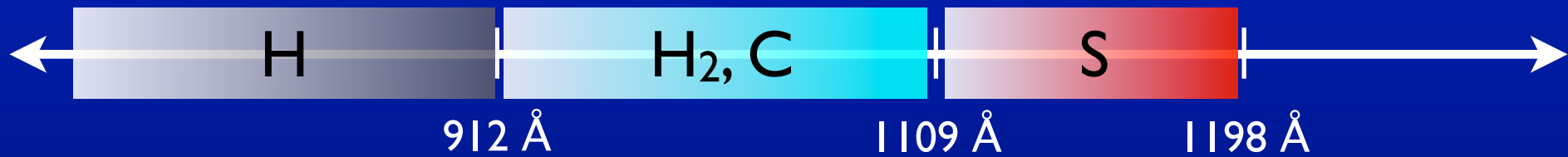
X-rays + PAHs =  
 weak accretion



Perez-Becker & EC 11ab

$a [\text{AU}]$

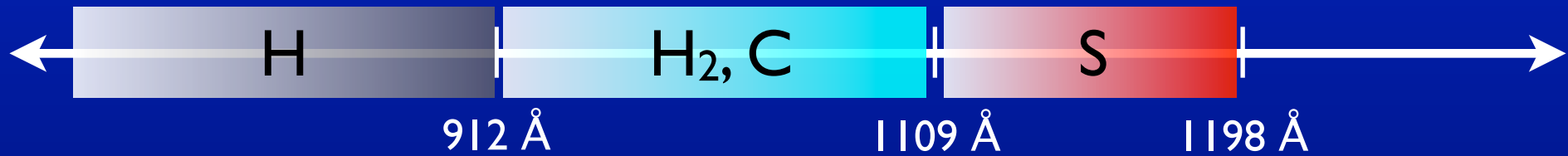
# Far-Ultraviolet (FUV) Ionization



$L_{\text{FUV}} \sim 10^{30}-10^{32}$   
erg/s

**HST + FUSE**  
(Bergin et al. 03; Herczeg et al. 02)

# FUV Ionization



## Strömgren slab

photoionizations      recombinations

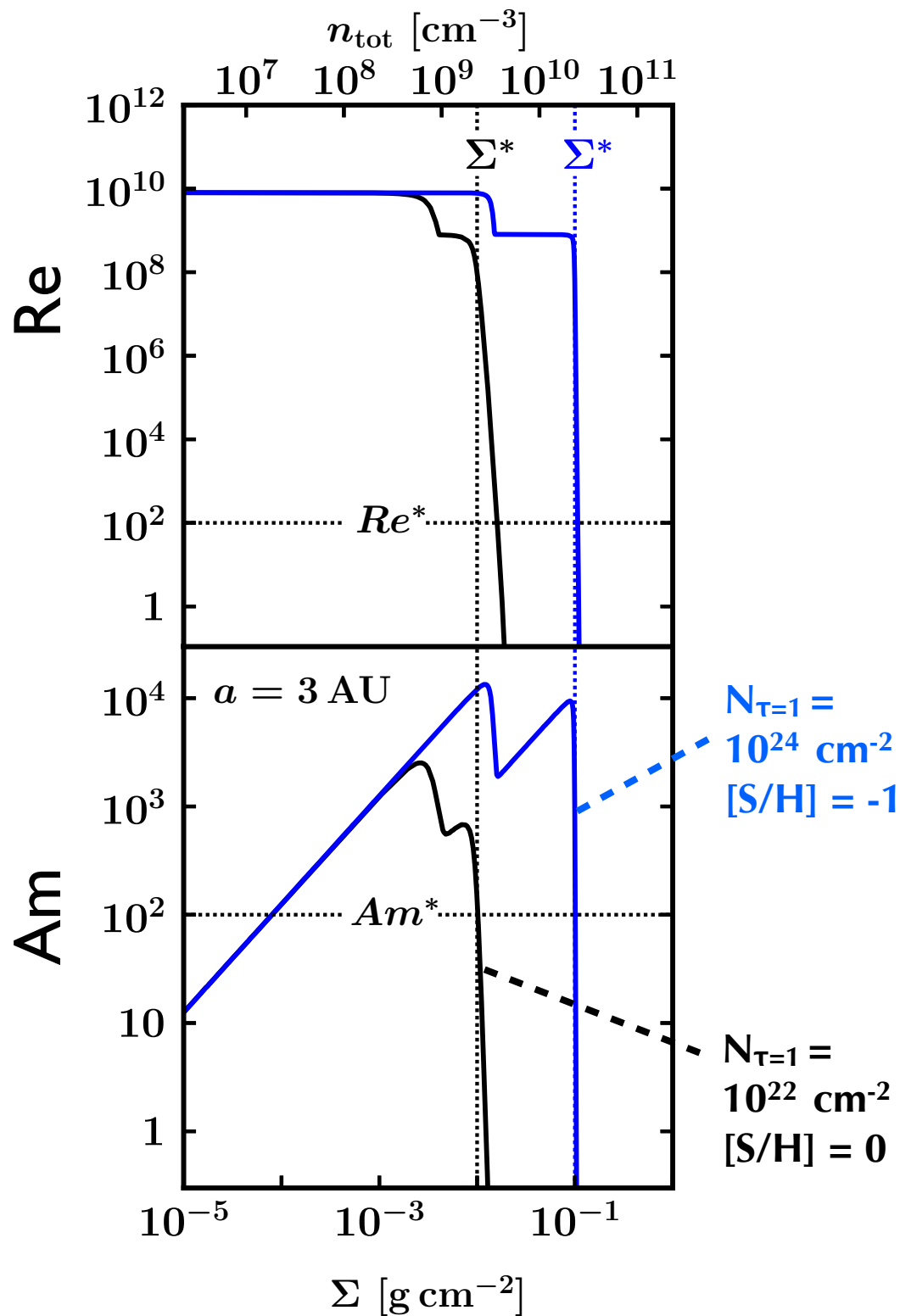
$$\frac{L_{\text{FUV}}}{h\nu 4\pi a^2} \cdot \frac{h}{a} \sim n_i n_e \alpha_{\text{rec}} \cdot h$$

$$n_i = n_e = f n_{\text{H}_2} \text{ (cosmic abundance)}$$

$n_{\text{H}_2}$

$$\Rightarrow \Sigma_{\text{MRI}} \sim n_{\text{H}_2} \mu h$$

$$\sim 0.1 \left( \frac{L_{\text{FUV}}}{10^{30} \text{ erg/s}} \right)^{1/2} \left( \frac{10^{-5}}{f} \right) \text{ g/cm}^2$$

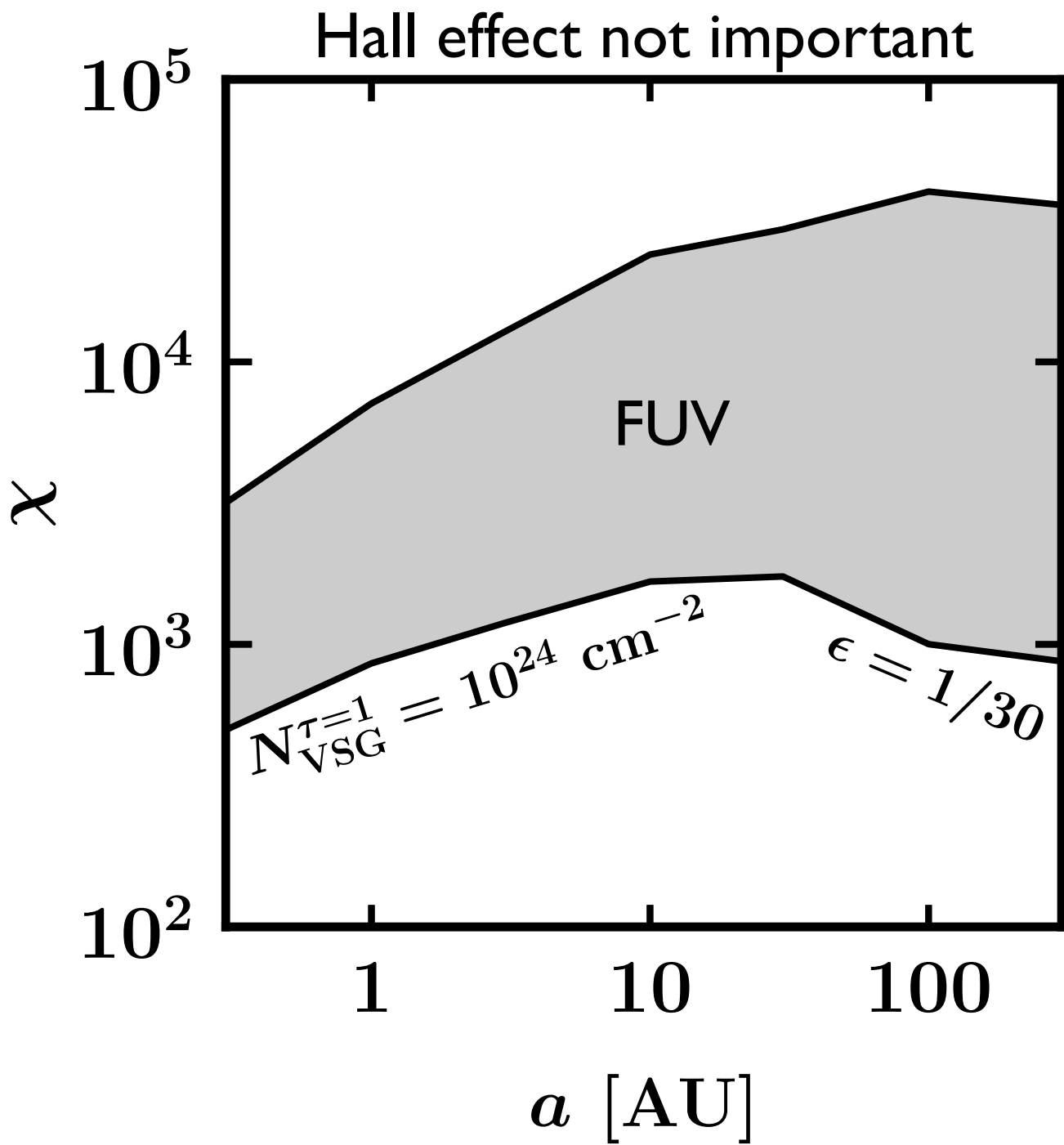


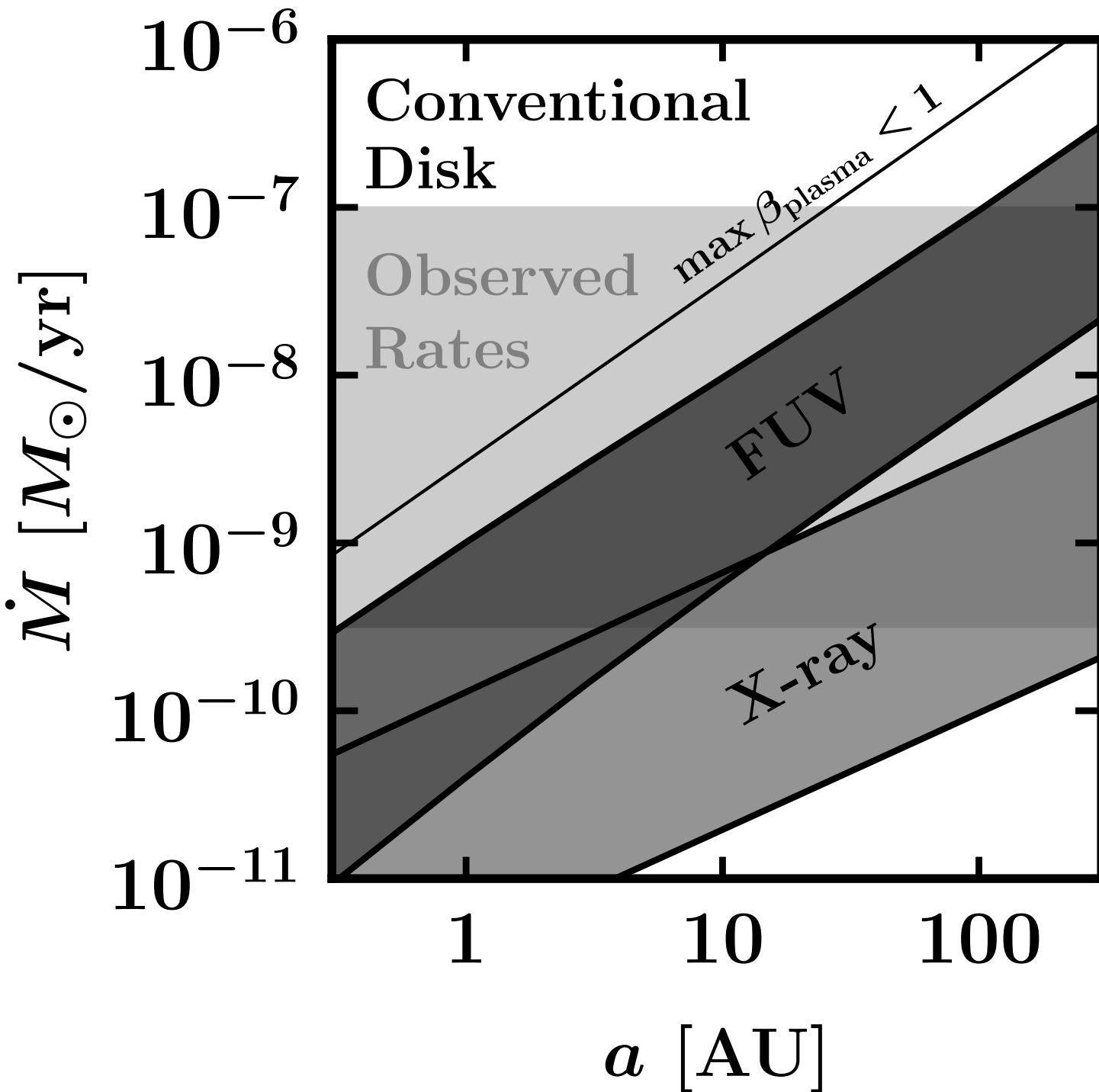
FUV ionization only

Field is frozen to plasma ✓  
 Good ion-neutral coupling ✓

robust against PAHs  
 (PAHs included at  
 maximum abundance)

sensitive to dust-to-gas ratio  
 (vertical settling of dust)





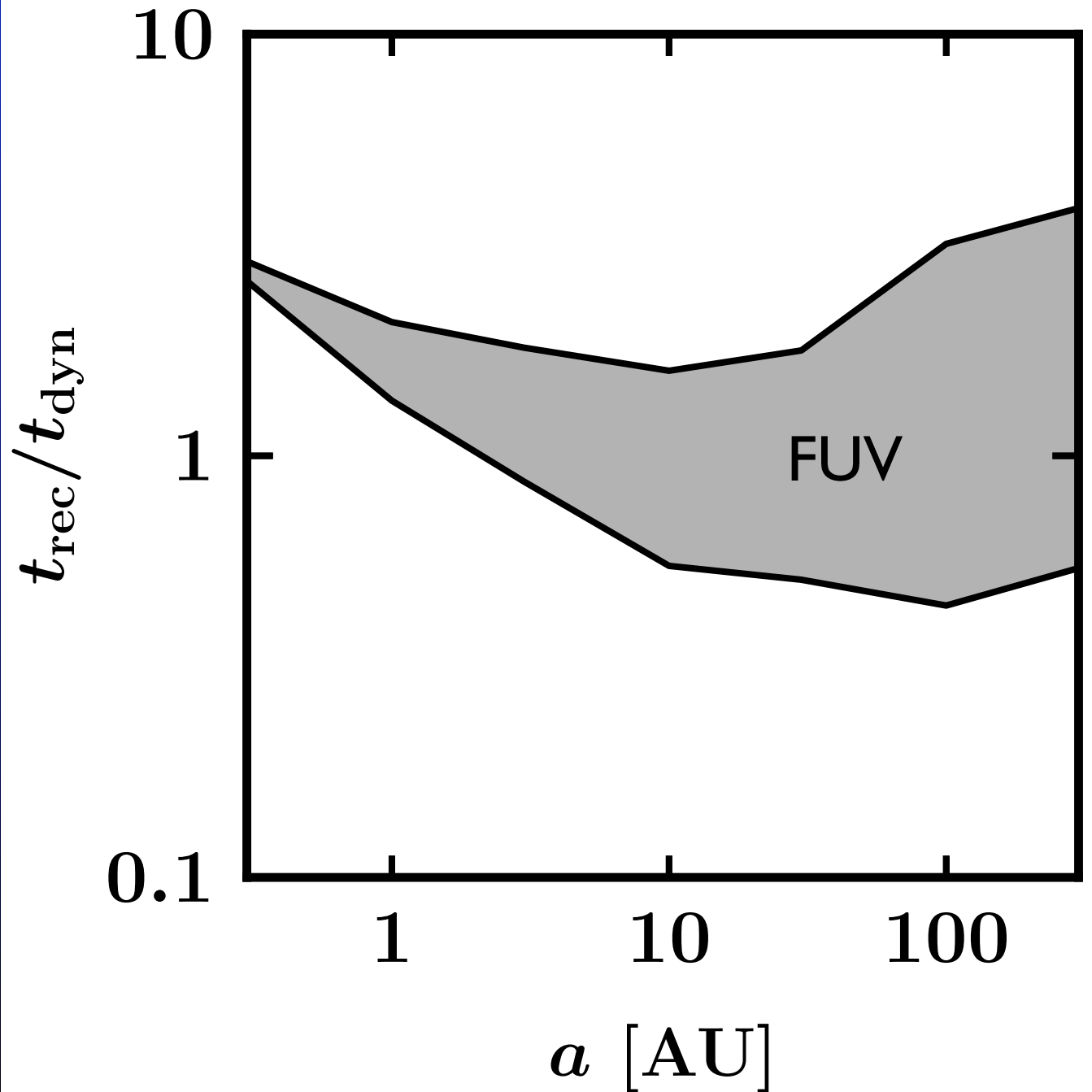
$$\dot{M} \sim 2 \times 3\pi \Sigma^* \nu$$

$$\sim 6\pi \Sigma^* \alpha \frac{kT}{\mu\Omega}$$

FUV-ionized  
surface layers  
can reproduce  
accretion rates  
at large radius  
but not  
small radius

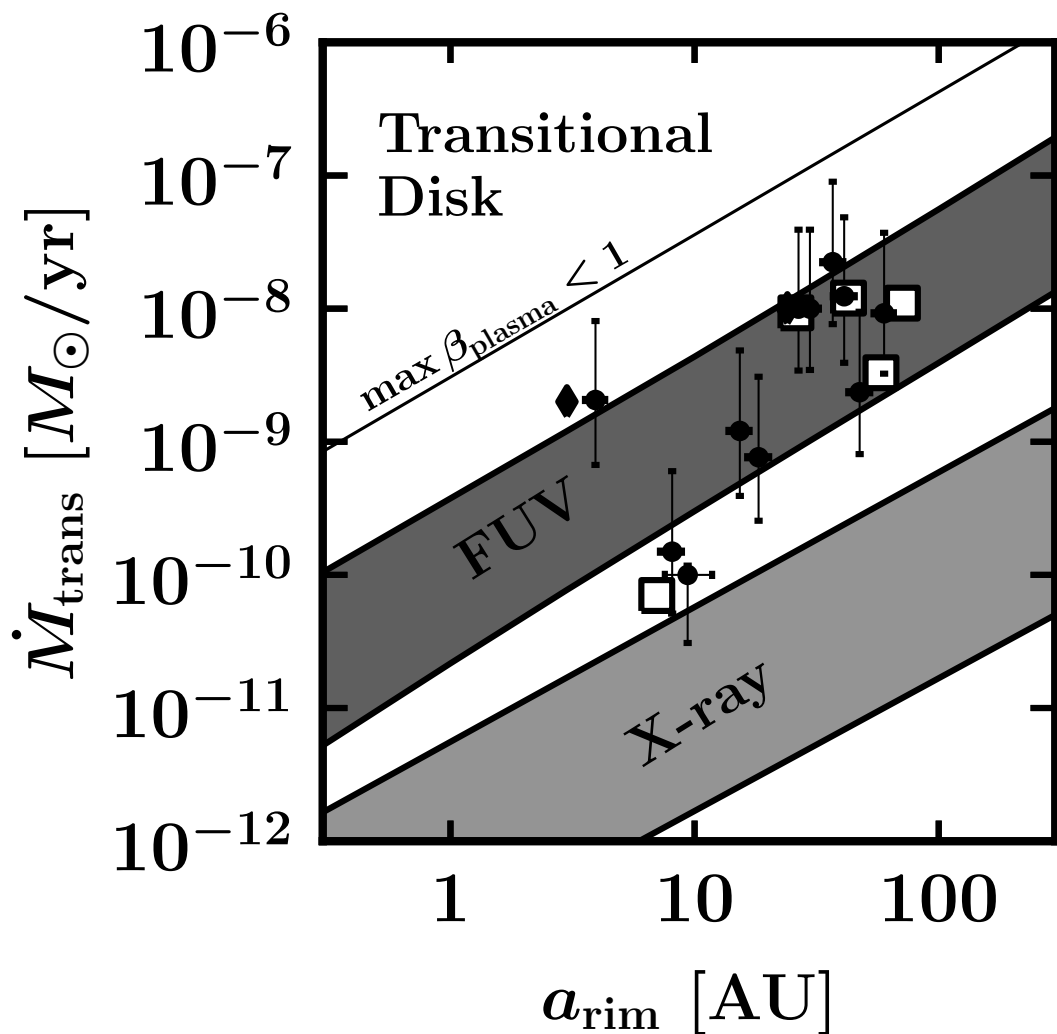
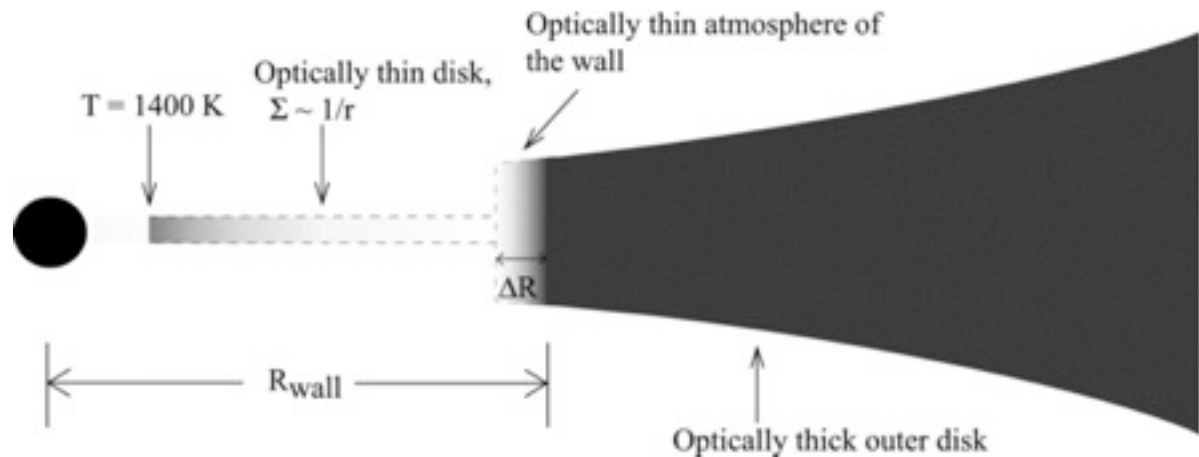
Ion recombination  
time  
vs.  
dynamical time

Turbulent mixing  
of plasma to  
greater depths  
can extend  
MRI-active layer





# FUV-driven MRI in Transitional Disks



Rim accretion rate reproduces observations

Transport problem at small radii could be solved by companions

Murray-Clay & EC 07

Kim et al. 09

Perez-Becker & EC 11ab

Zhu et al. 11

Extra Slides

Is the required field super-equipartition?

On the one hand, the field must be strong enough:

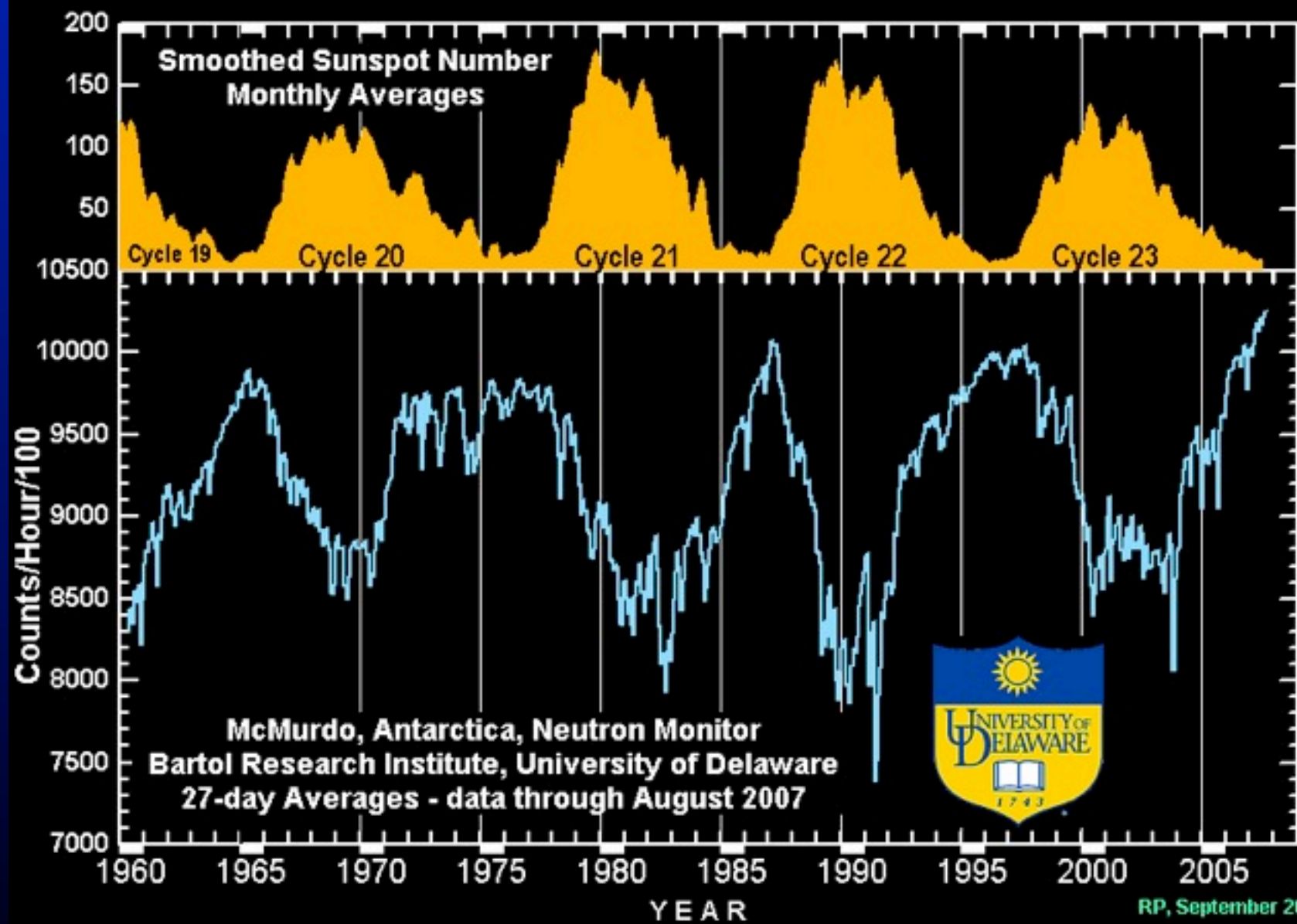
$$\dot{M} \sim \langle B_r B_\phi \rangle h / \Omega$$

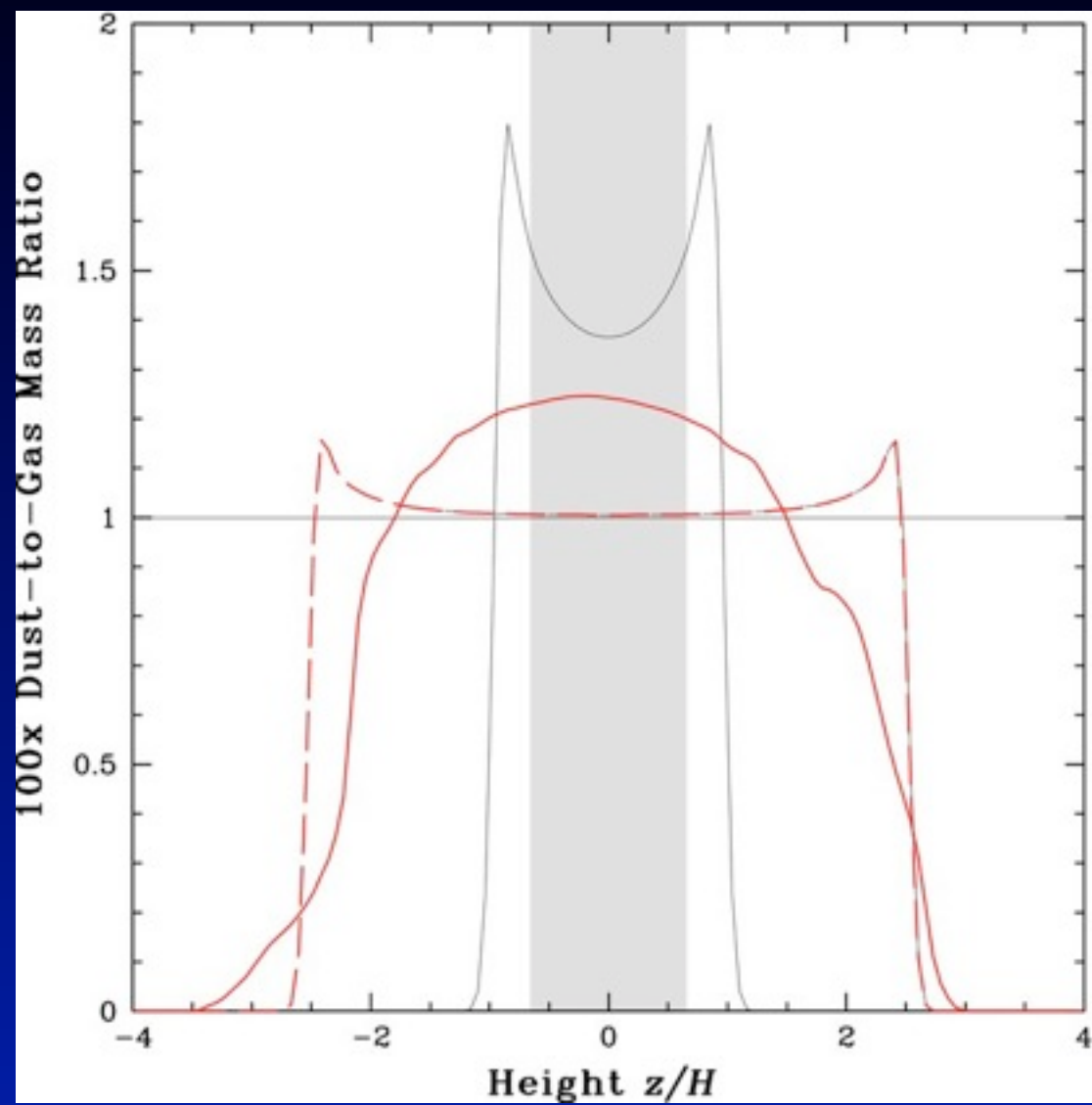
$$\Rightarrow \min B > 1 \text{ G} \left( \frac{\dot{M}}{10^{-8} M_\odot / \text{yr}} \right)^{1/2} \left( \frac{r}{\text{AU}} \right)^{-5/4}$$

$$\beta \equiv \frac{P_{\text{gas}}}{P_{\text{mag}}} = \frac{8\pi n k T}{B^2} < 1 \left( \frac{\Sigma}{0.1 \text{ g/cm}^2} \right) \left( \frac{10^{-8} M_\odot / \text{yr}}{\dot{M}} \right) \left( \frac{r}{1 \text{ AU}} \right)$$

On the other hand the field cannot be too strong:  $\beta > 1$

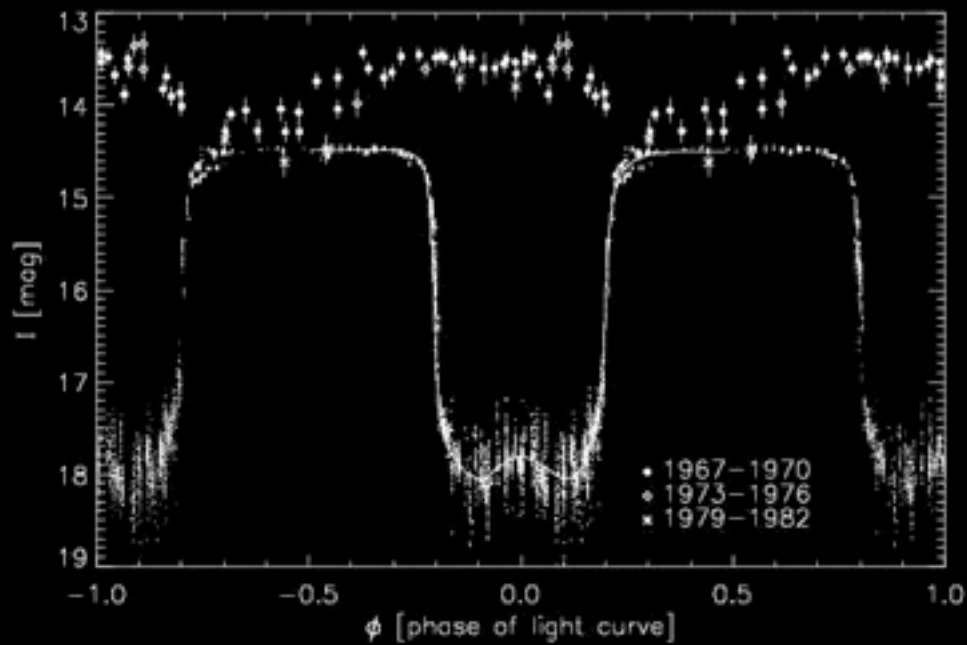
Possible for  $r > 1 \text{ AU}$



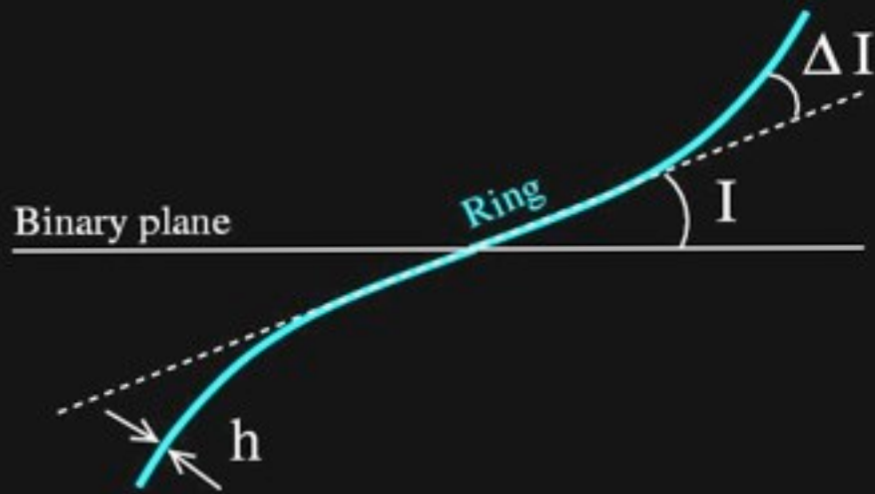


# Inside-Out Accretion of Transitional Disks

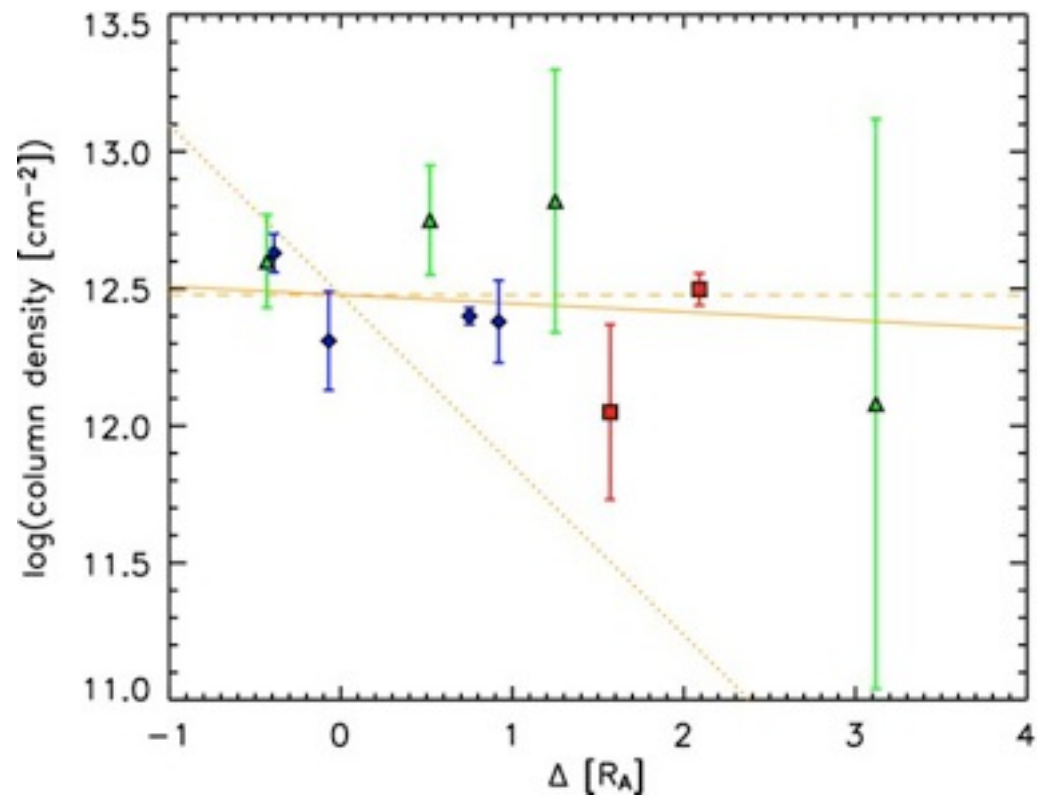




Measuring dust layer thicknesses  
(e.g., occulting circumbinary disk of KH 15D)



- Dust thickness  $h/r \leq R_{\odot}/r \sim 10^{-2}$
- Inclination  $I \sim 10^{-1}$
- Warp  $\Delta I / I < 10^{-1}$  (self-gravity)  
 $\Delta I / I \sim -10^{-1}$  (gas pressure)

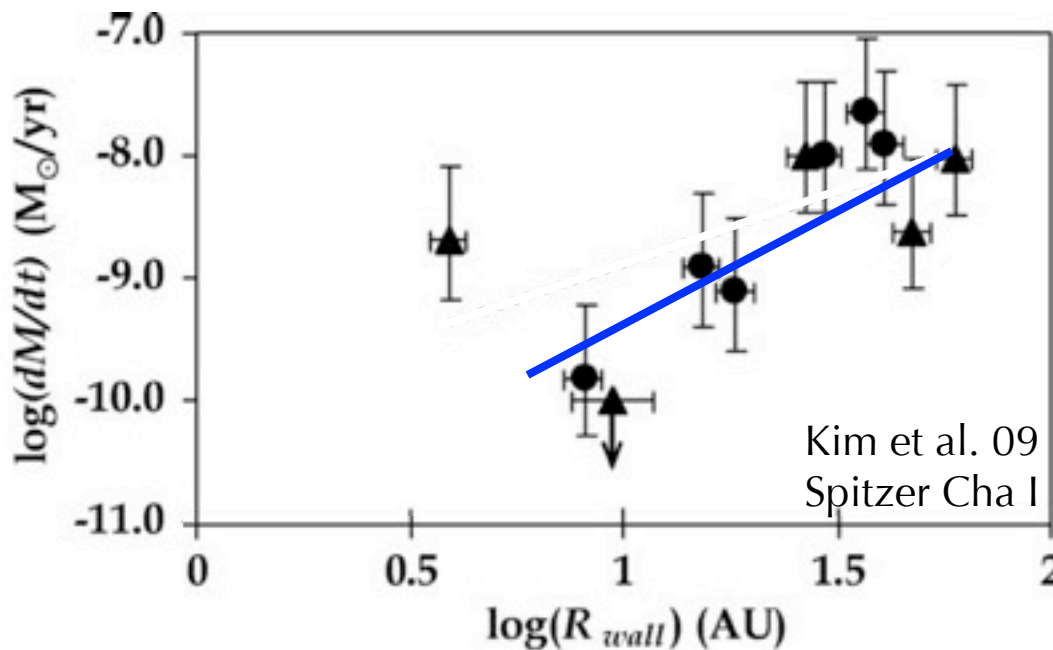
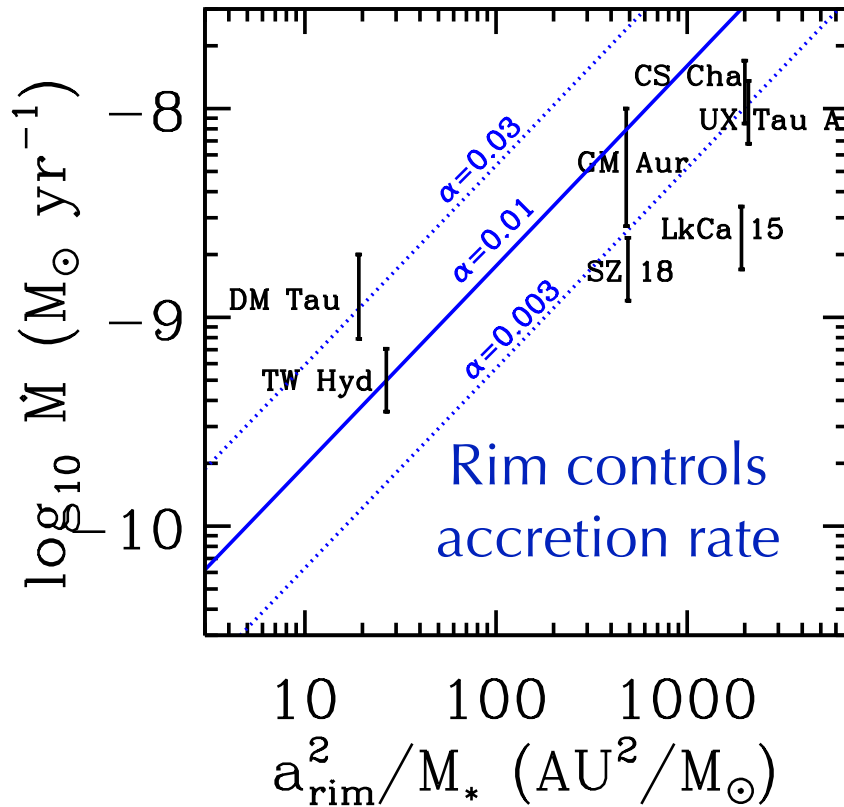


## X-ray driven MRI

$$\dot{M} \sim \frac{12\pi\alpha N^* a_{\text{rim}}^2 (kT^*)^{3/2}}{GM_* \mu^{1/2}}$$

For constant  $\alpha$ ,

$$\Sigma_{\text{gas}} \sim 10 - 100 \text{ g cm}^{-2} \text{ @ 1 AU}$$

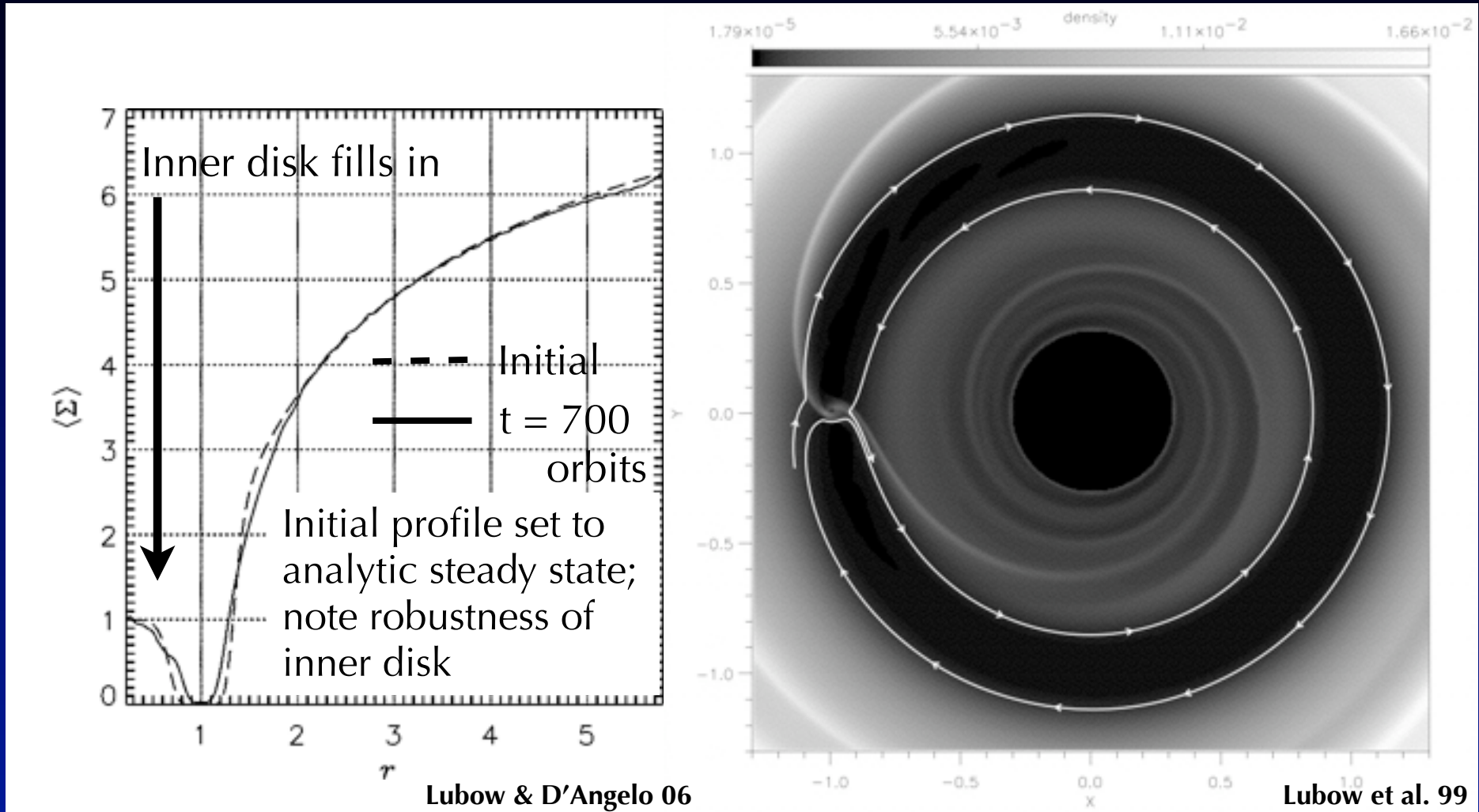


- 10-100 x lower density than MMSN
- Satisfies CO lower limits
- Type II migration slower than usual

But cannot explain origin of hole



# Planet Clearing



$\dot{M}_{\text{inner}} \approx 0.1 \dot{M}_{\text{outer}}$   
neglecting  
migration

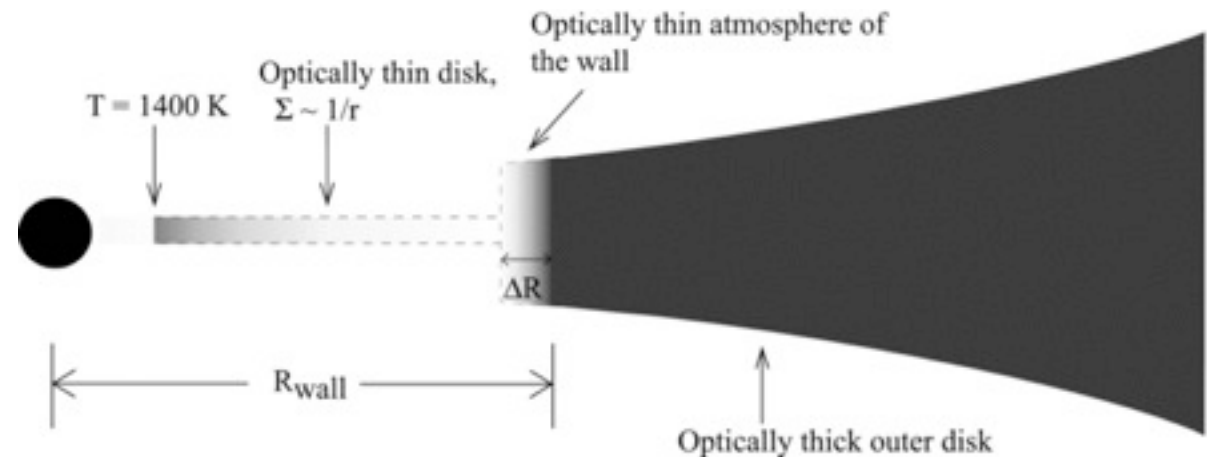
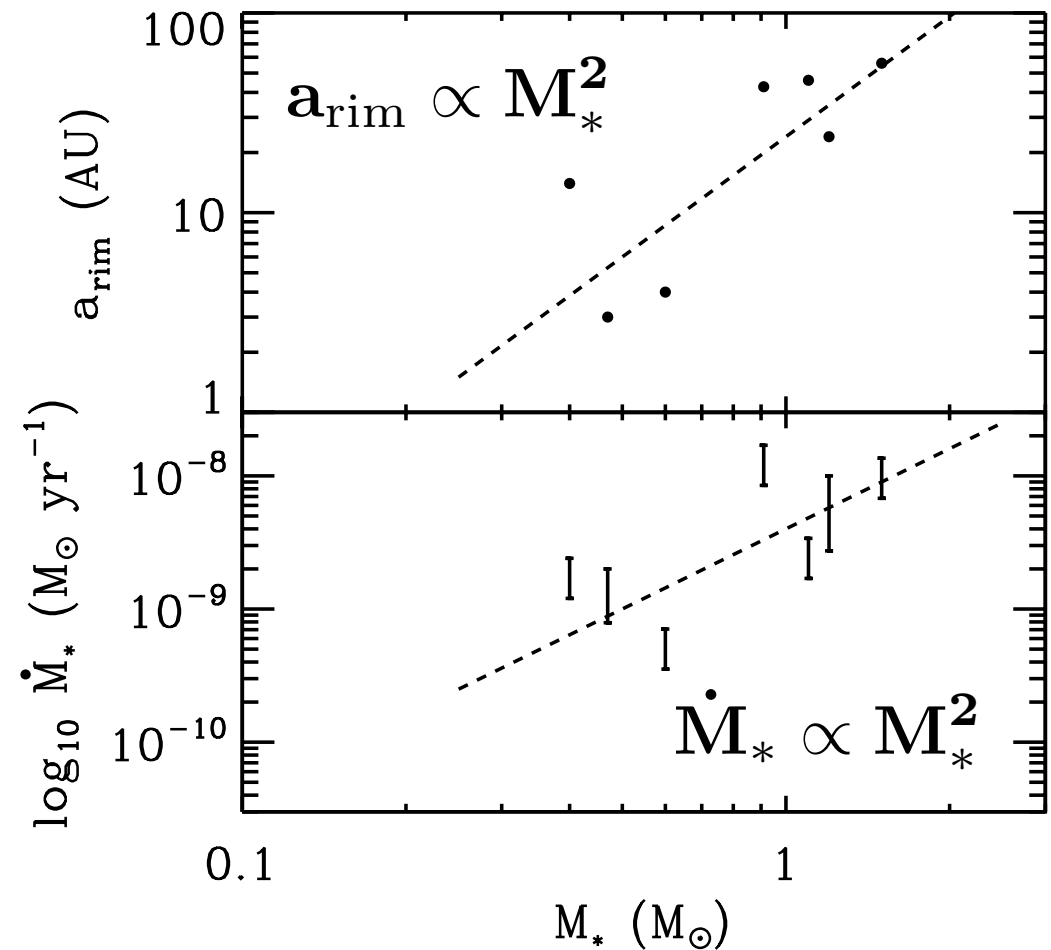
- But planetary migration reduces clearing efficiency
- Short-lived solution ( $t_{\text{diffusion}} \sim r^2 / \nu \sim 10^4$  orbits)
- Perhaps multiple planets can help

But deeper correlations  
may exist ...

Same  
 $\dot{M}_* \propto M_*^2$   
holds for  
non-transitional  
disks

How to keep the  
inner hole  
clear of dust?

Leaked dust might  
concentrate at  $a \ll a_{\text{rim}}$ ,  
restoring  $\tau_{10\mu\text{m}} > 1$ :  
Gapped  
("pre-transitional") disk  
possible



# Inside-Out MRI

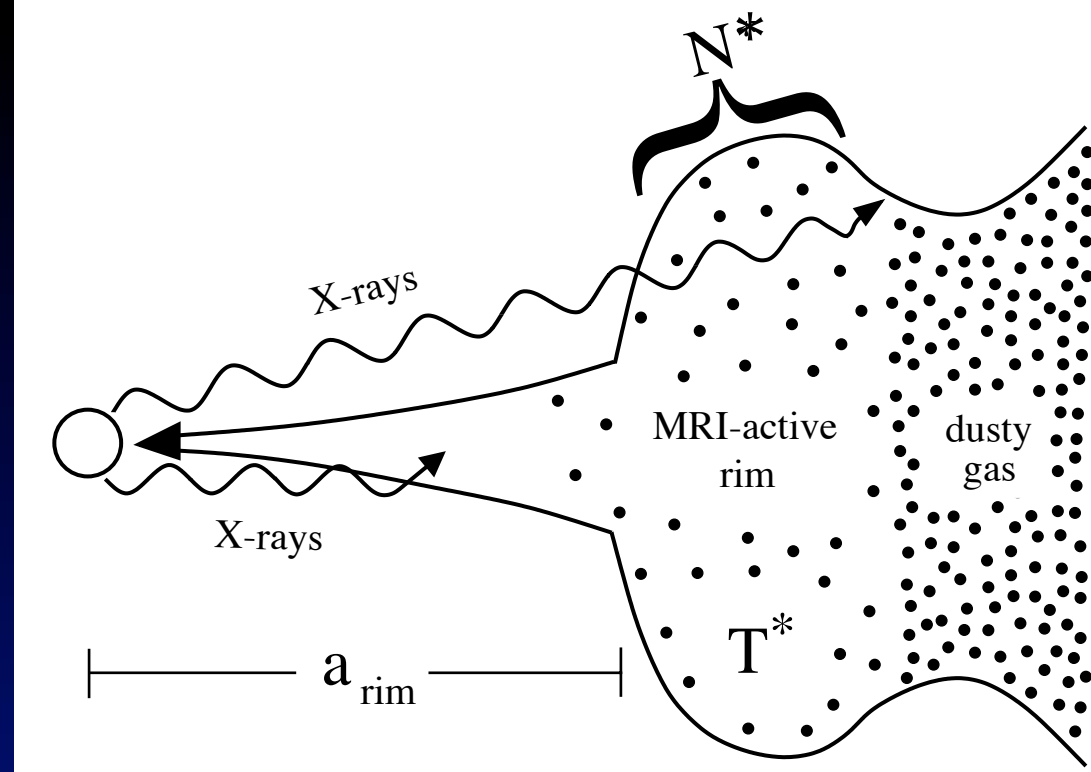
$$M_{\text{rim}} = 2\pi a_{\text{rim}} \times 2h \times N^* \mu$$

$10^{23} \text{ cm}^{-2}$

$$t_{\text{diff}} \sim a_{\text{rim}}^2 / \nu$$

$$\nu = \alpha c_s h$$

MRI simulations give  $10^{-4}$ - $10^{-1}$



$$\dot{M} \sim \frac{M_{\text{rim}}}{t_{\text{diff}}} \sim \frac{12\pi\alpha N^* a_{\text{rim}}^2 (k T^*)^{3/2}}{GM_* \mu^{1/2}}$$

230 K

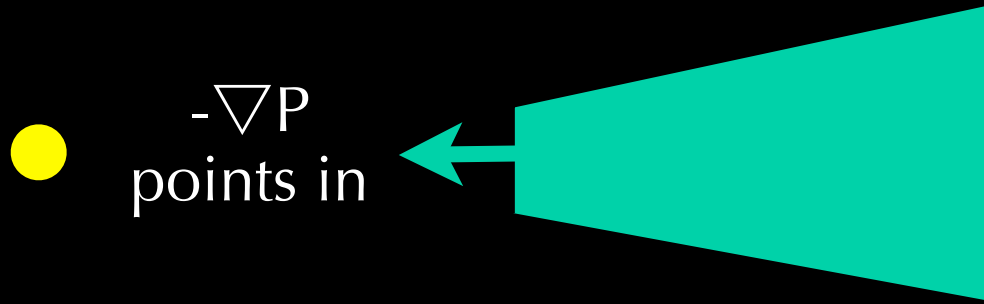
$$\frac{L_X \sigma_X e^{-N^* \sigma_X} f_{\text{heat}} n}{4\pi a_{\text{rim}}^2} \sim \Lambda_{\text{CO}}(T^*)$$

photo-ionization heating

CO ro-vibrational cooling

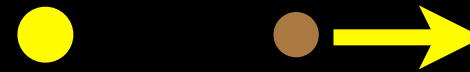
# Keeping inner hole clear of dust

## Aerodynamic filter



Gas is super-Keplerian  
 Dust is Keplerian  $\therefore$  dragged out

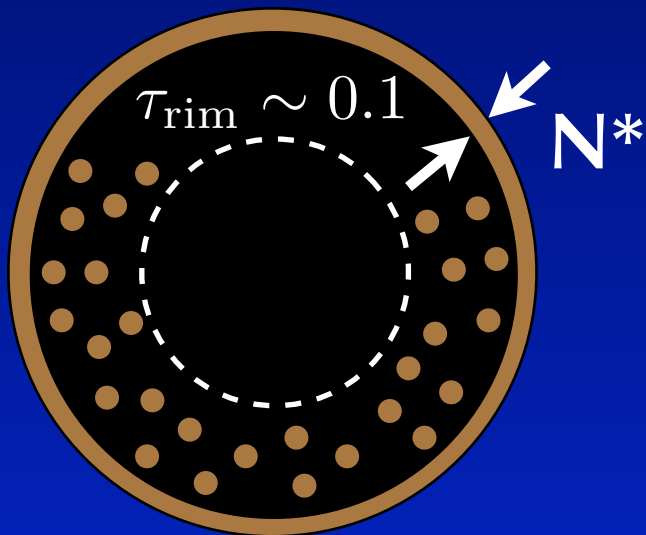
## Radiation pressure



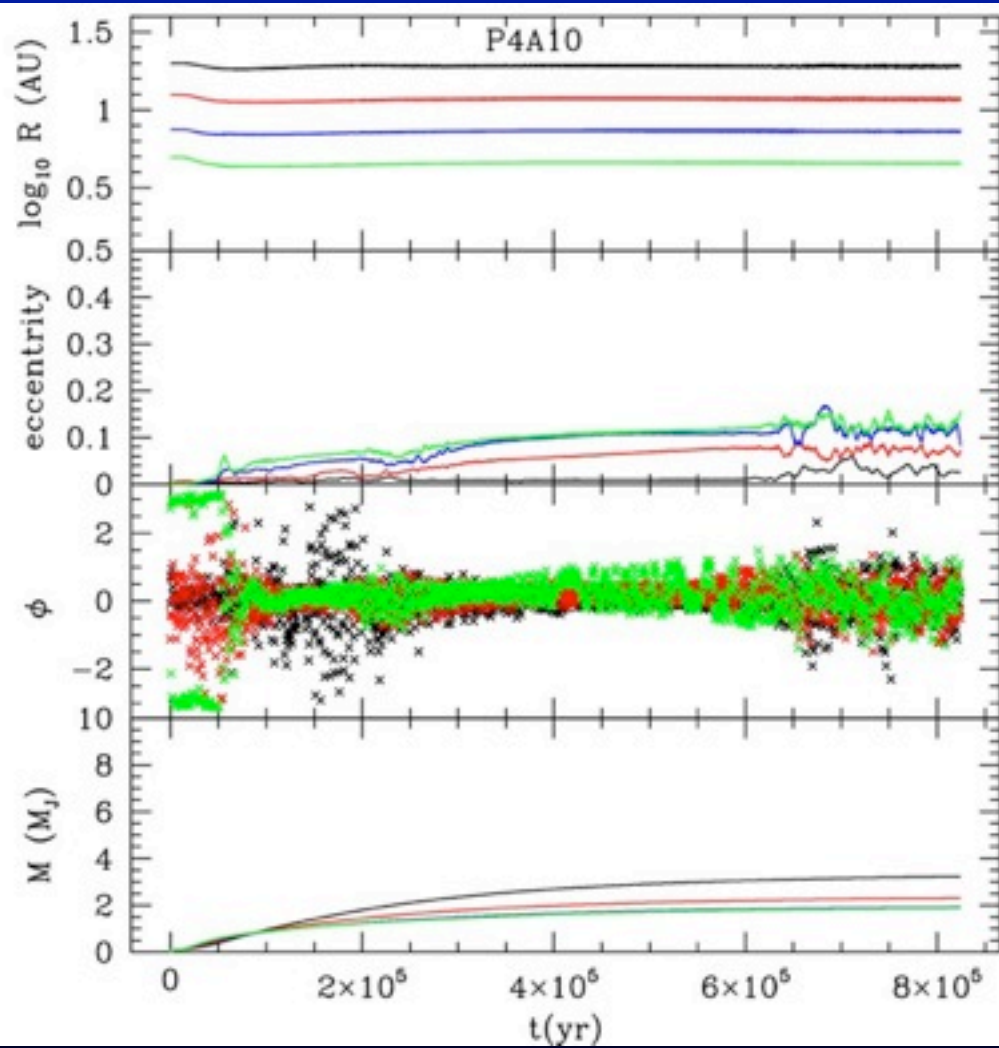
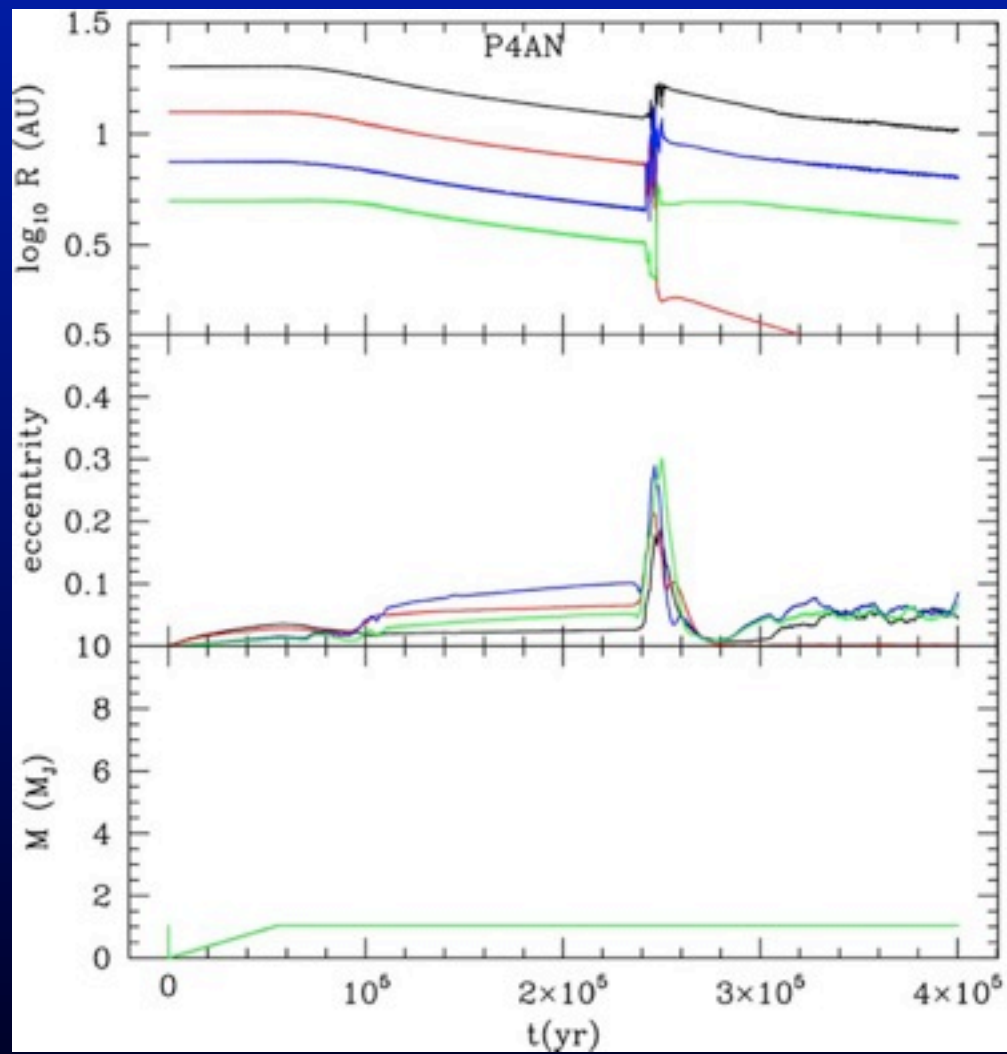
$$t_{\text{blow}} \sim \frac{1}{\Omega} \left( \frac{1}{\Omega t_{\text{stop}}} \right)$$

Rice et al. 06

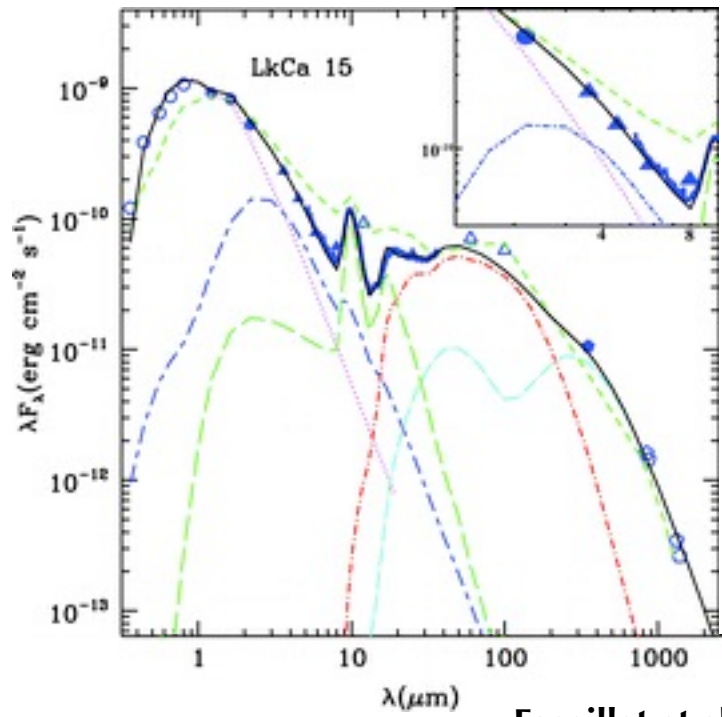
EC & Murray-Clay 07



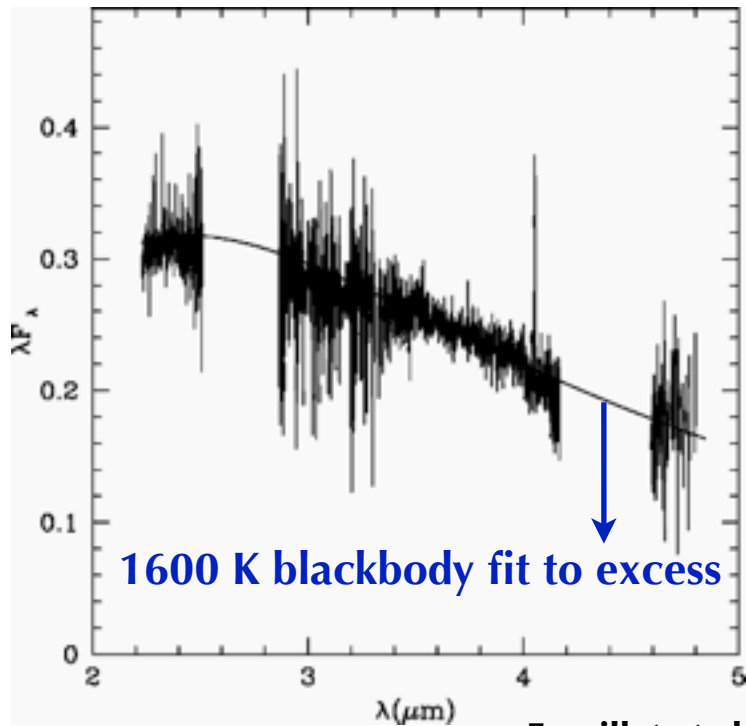
- Filtering is inefficient
- Leaked dust might concentrate at  $a \ll a_{\text{rim}}$ , restoring  $\tau_{10\mu\text{m}} > 1$ :  
 Gapped (“pre-transitional”) disk possible



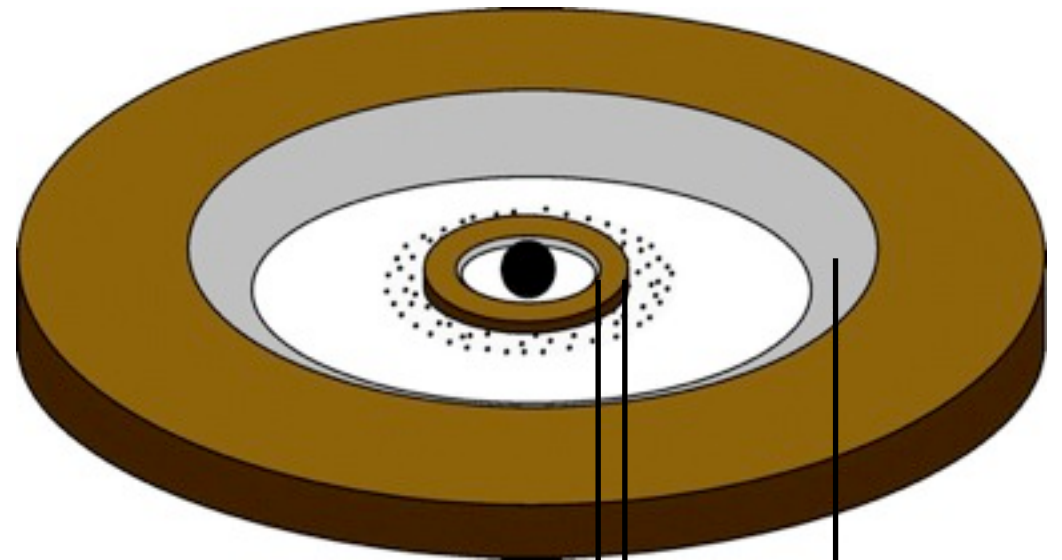
# “Pre-Transitional” Gapped Disks



Espaillet et al. 07



Espaillet et al. 08



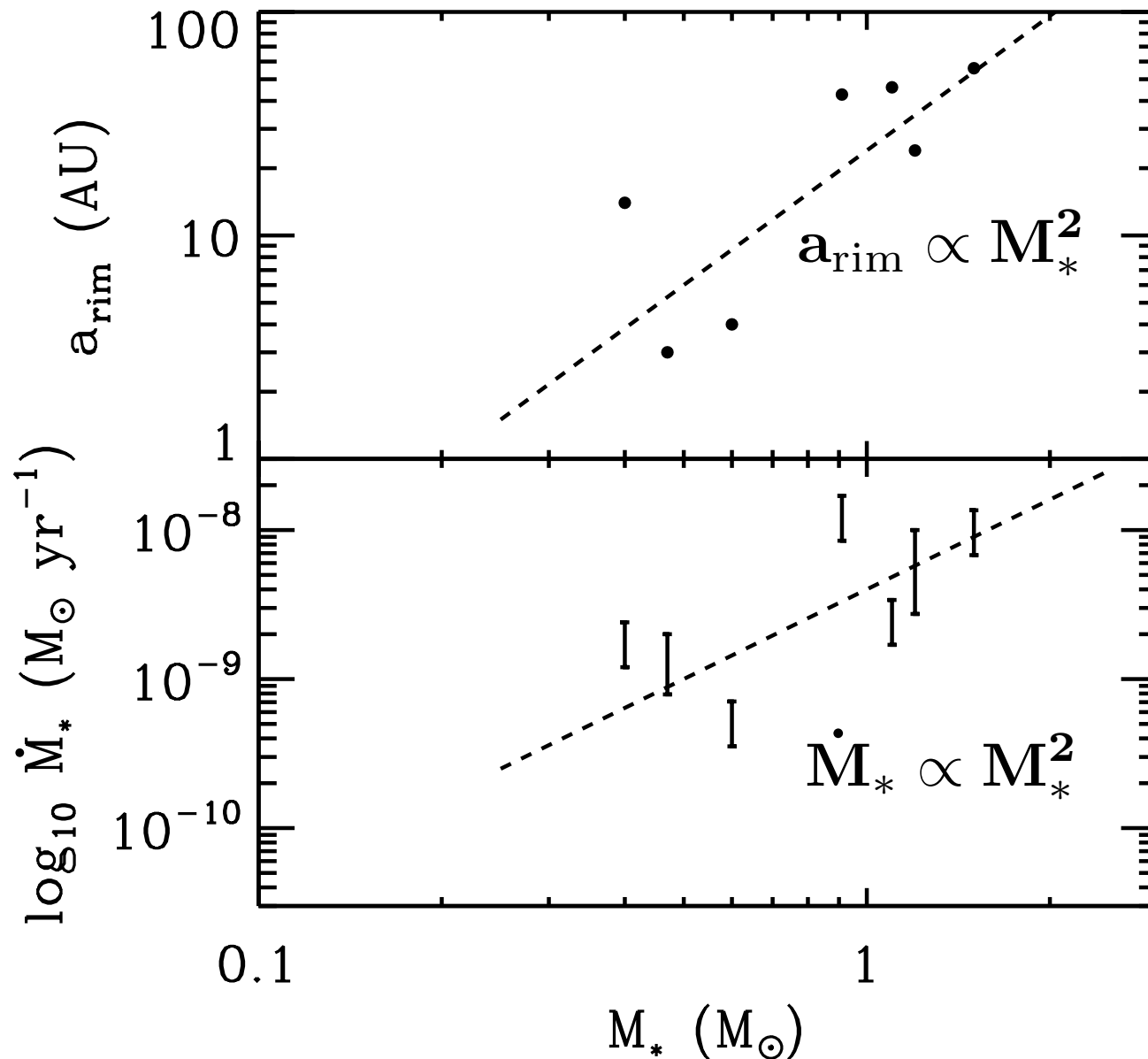
LkCa 15

0.12 AU

< 0.15 AU

46 AU

But deeper correlations may exist ...



Why?

And does similar relation hold for debris disks?

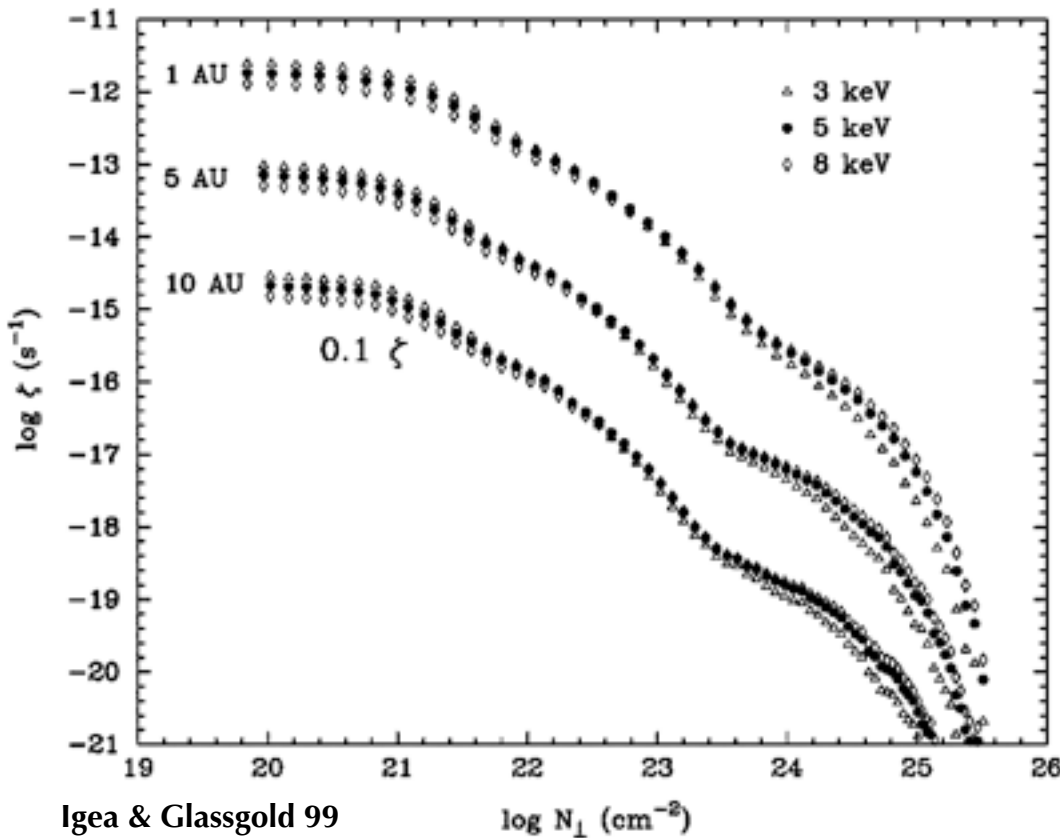
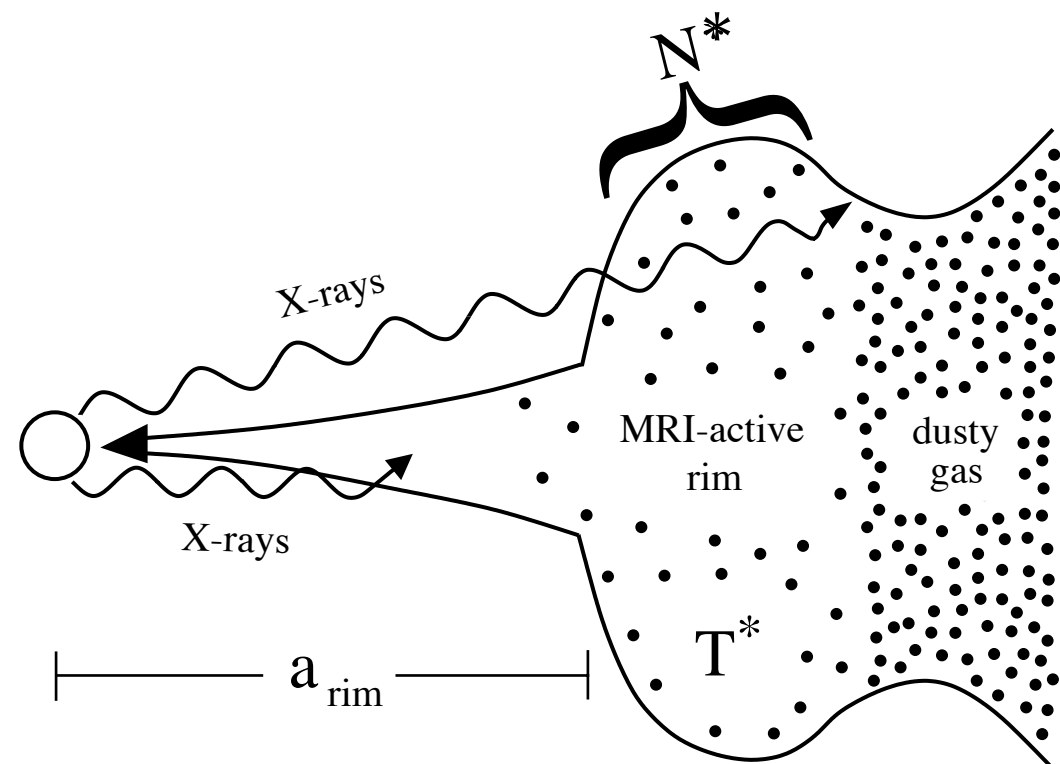
Same  $\dot{M}_* \propto M_*^2$  holds for non-transitional disks

# Sustaining MRI at $a \ll a_{\text{rim}}$

Scale to minimum temperature (blackbody)

$$T = 50 \text{ K } a_{\text{AU}}^{-3/4} \dot{M}_{-9}^{1/4} \hat{T} \quad (\hat{T} > 1)$$

$$N_{\perp} = 10^{25} \text{ cm}^{-2} a_{\text{AU}}^{-3/4} \alpha_{0.01}^{-1} \dot{M}_{-9}^{3/4} \hat{T}^{-1}$$



Igea & Glassgold 99

$\zeta$  (Igea & Glassgold 99)

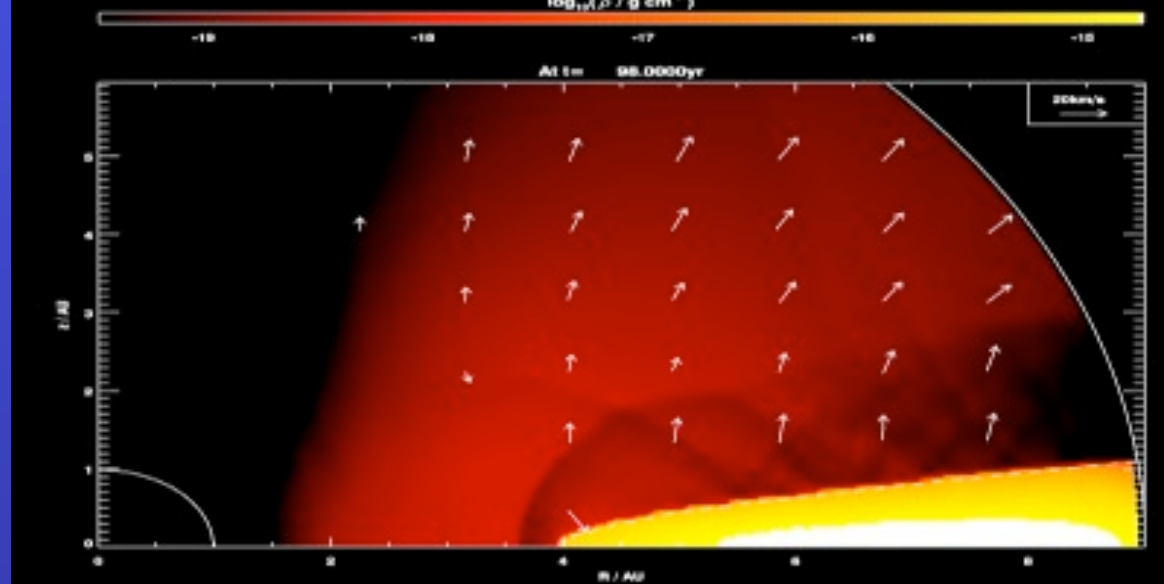
↓ quartic

$A_m \approx 90 @ 1 \text{ AU}$  vs.  $A_m^* \approx 100$   
 $A_m \approx 120 @ 0.1 \text{ AU}$

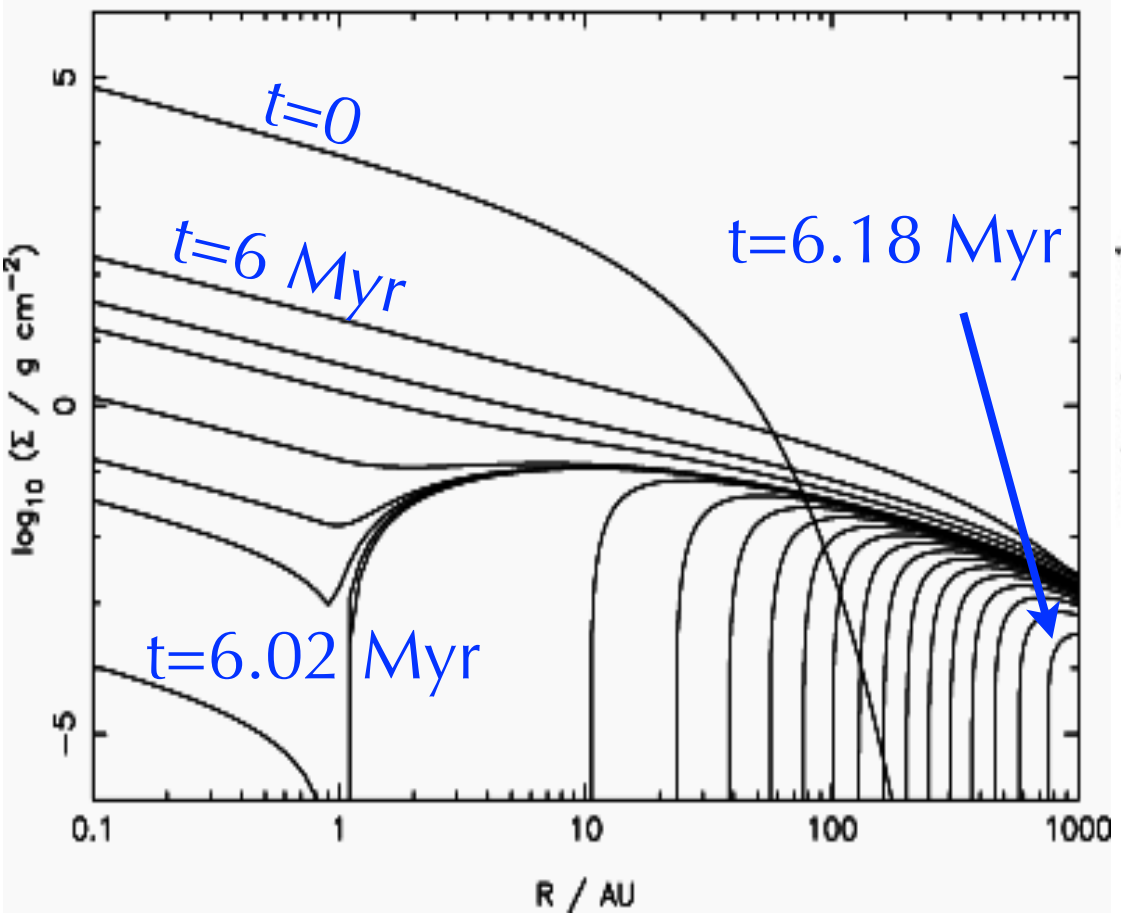
$\therefore$  Even midplane is MRI-active



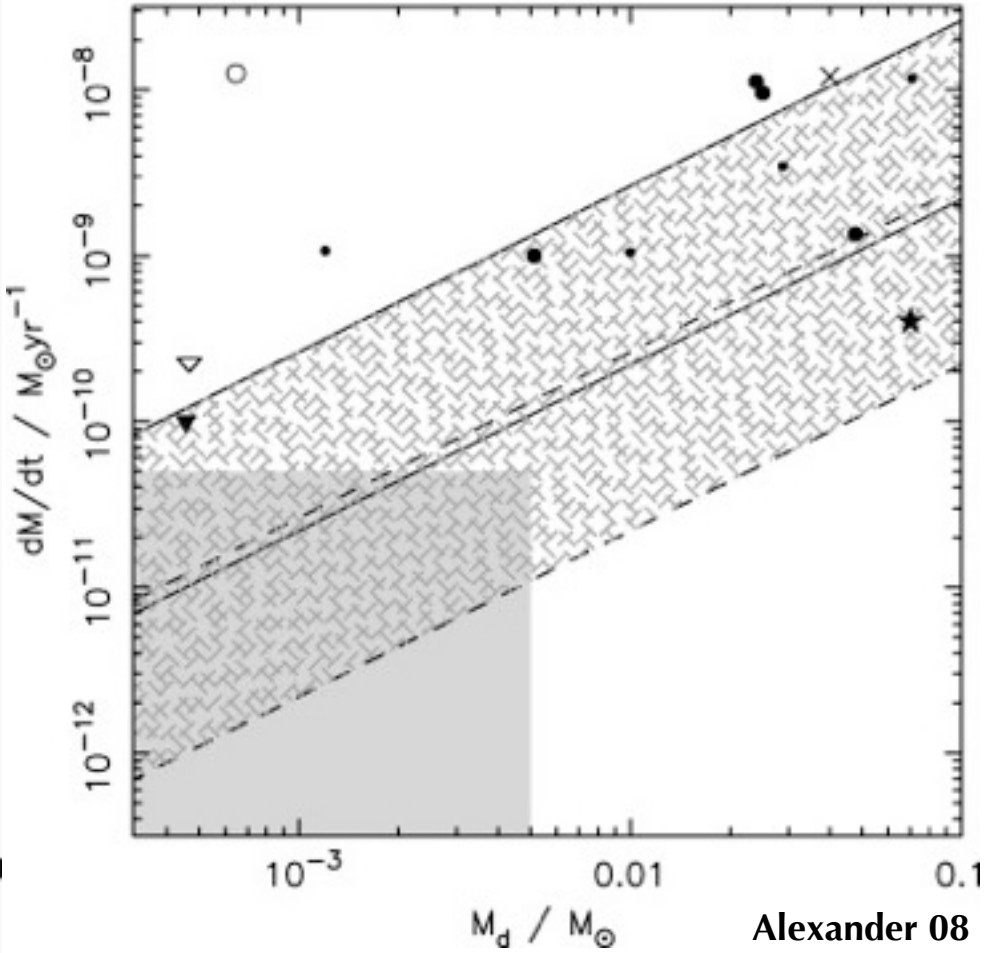
# Outer disk photoevaporation starves inner disk



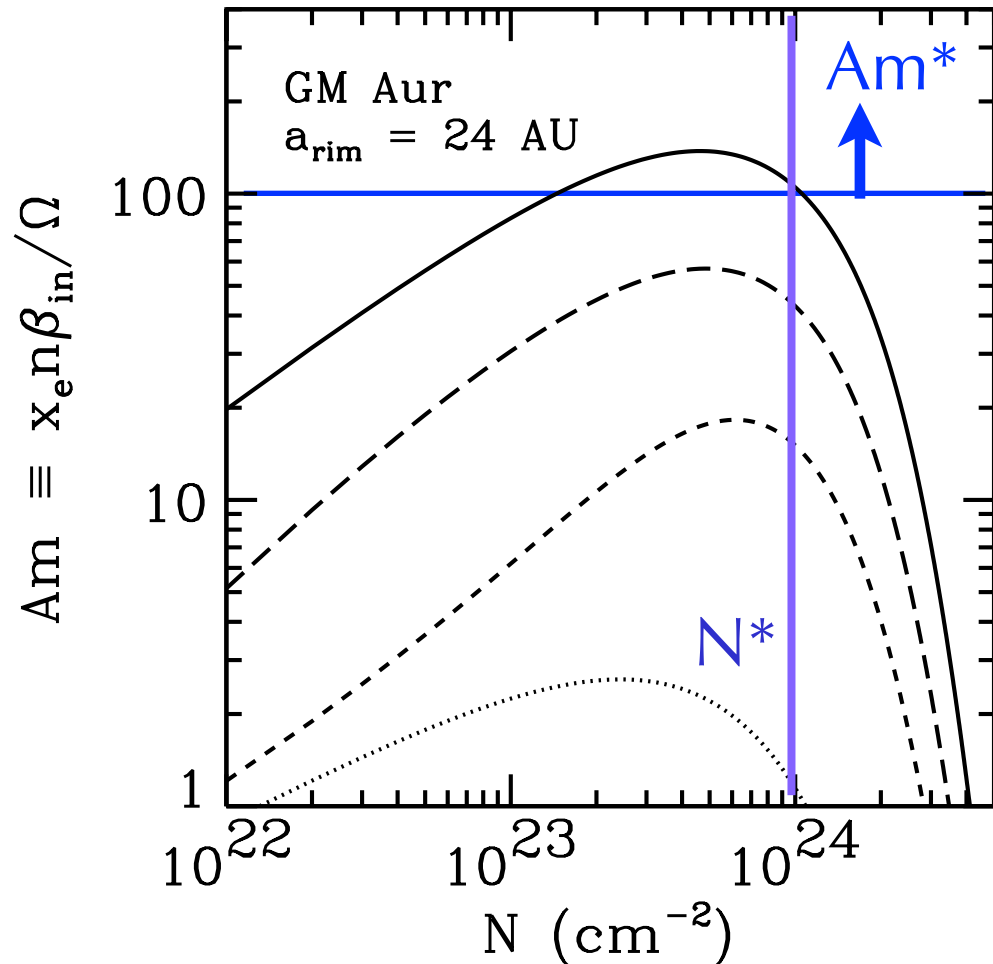
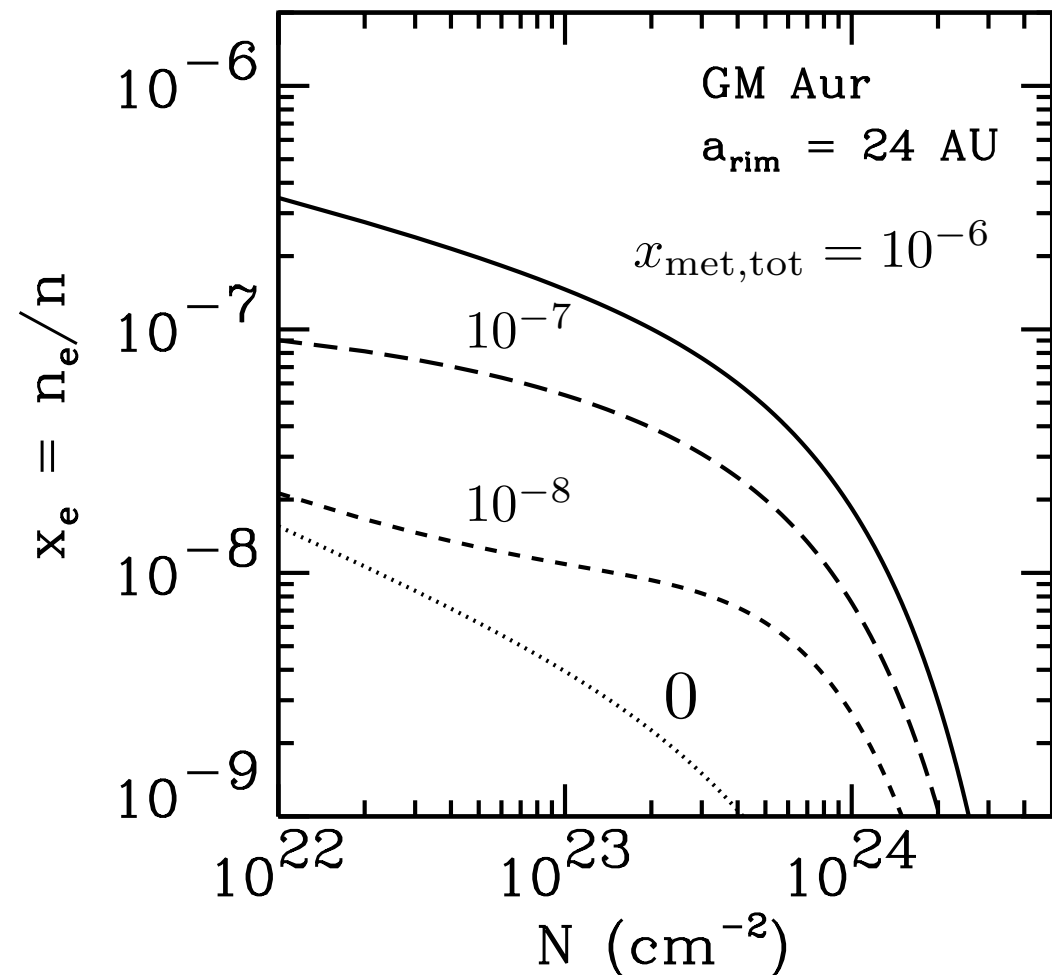
Evolution of surface density:  $M_* = 1M_\odot$ ,  $\phi = 10^{42} \text{s}^{-1}$



Properties of inner hole sources



# Estimating $N^*$



$$x_e^4 + \left( \frac{\beta_{\text{gr}}}{\beta_{\text{rec}}} \right) x_e^3 + \left( \frac{\zeta}{n \beta_{\text{diss}} \beta_{\text{rec}}} \right) x_e^2 - \left( \frac{\zeta}{n \beta_{\text{diss}} \beta_{\text{rec}}} \right) \left( \frac{\beta_{\text{gr}}}{\beta_t} + x_{\text{met,tot}} \right) x_e - \frac{\beta_t}{\beta_{\text{rec}}} \left( \frac{\zeta}{n \beta_{\text{diss}}} \right)^2 = 0$$

$$n = 2N/a_{\text{rim}} \quad \zeta = \frac{L_X \sigma_X e^{-N \sigma_X} \zeta_{\text{secondary}}}{4\pi E_X a_{\text{rim}}^2}$$

# Theories for transitional disks are not mutually exclusive

Planets + Grain growth + MRI + Radiative / aerodynamic blowout

smaller  $\dot{M}_*$

smaller  $\tau_{10\mu\text{m}}$

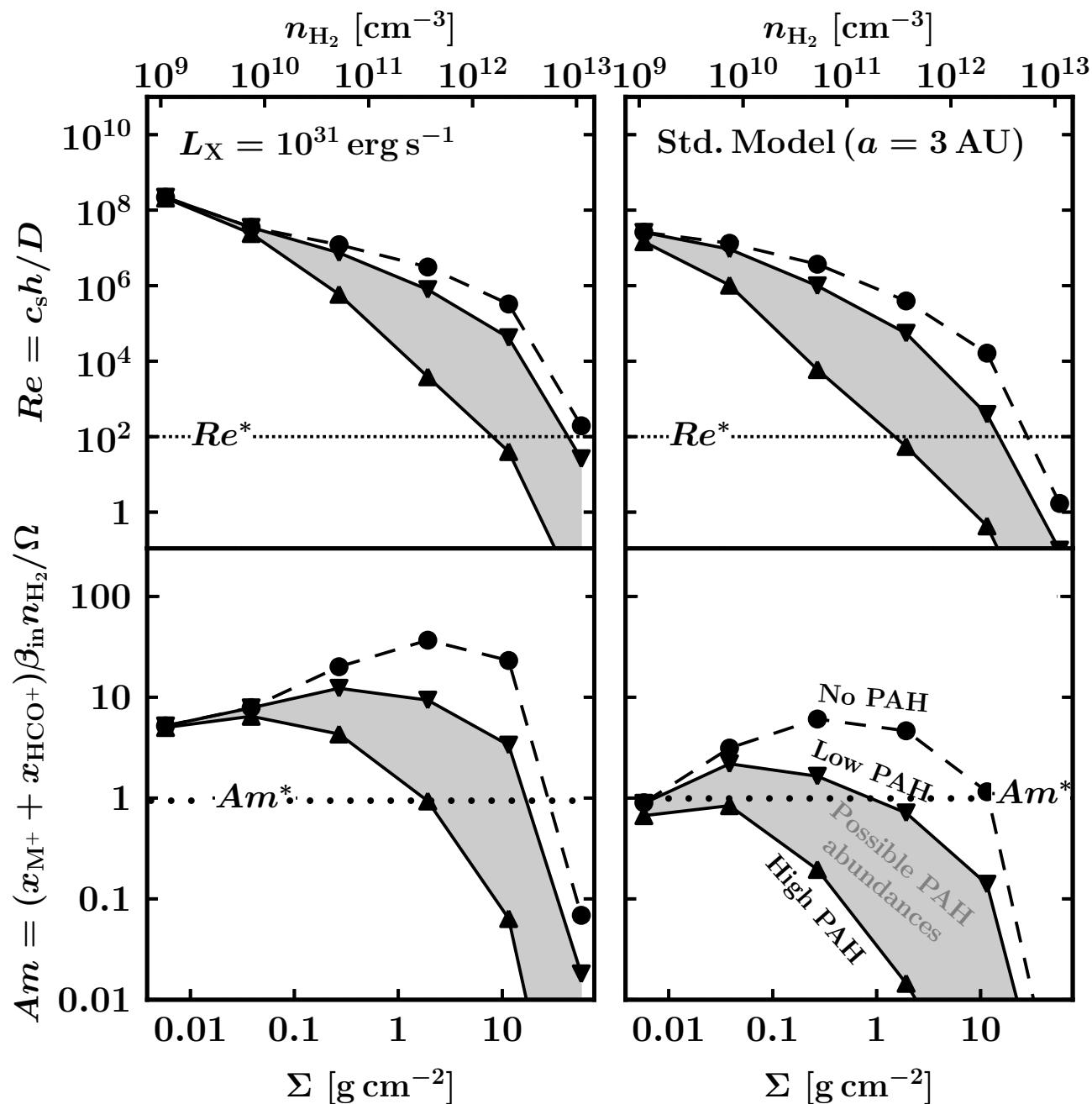
origin  
of viscosity

smaller  $\tau_{10\mu\text{m}}$

Multiple planets  
might explain  
factor of 10  
and prolong Type  
II migration

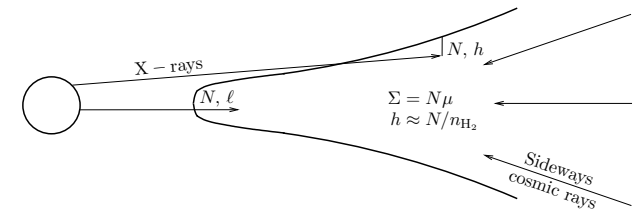
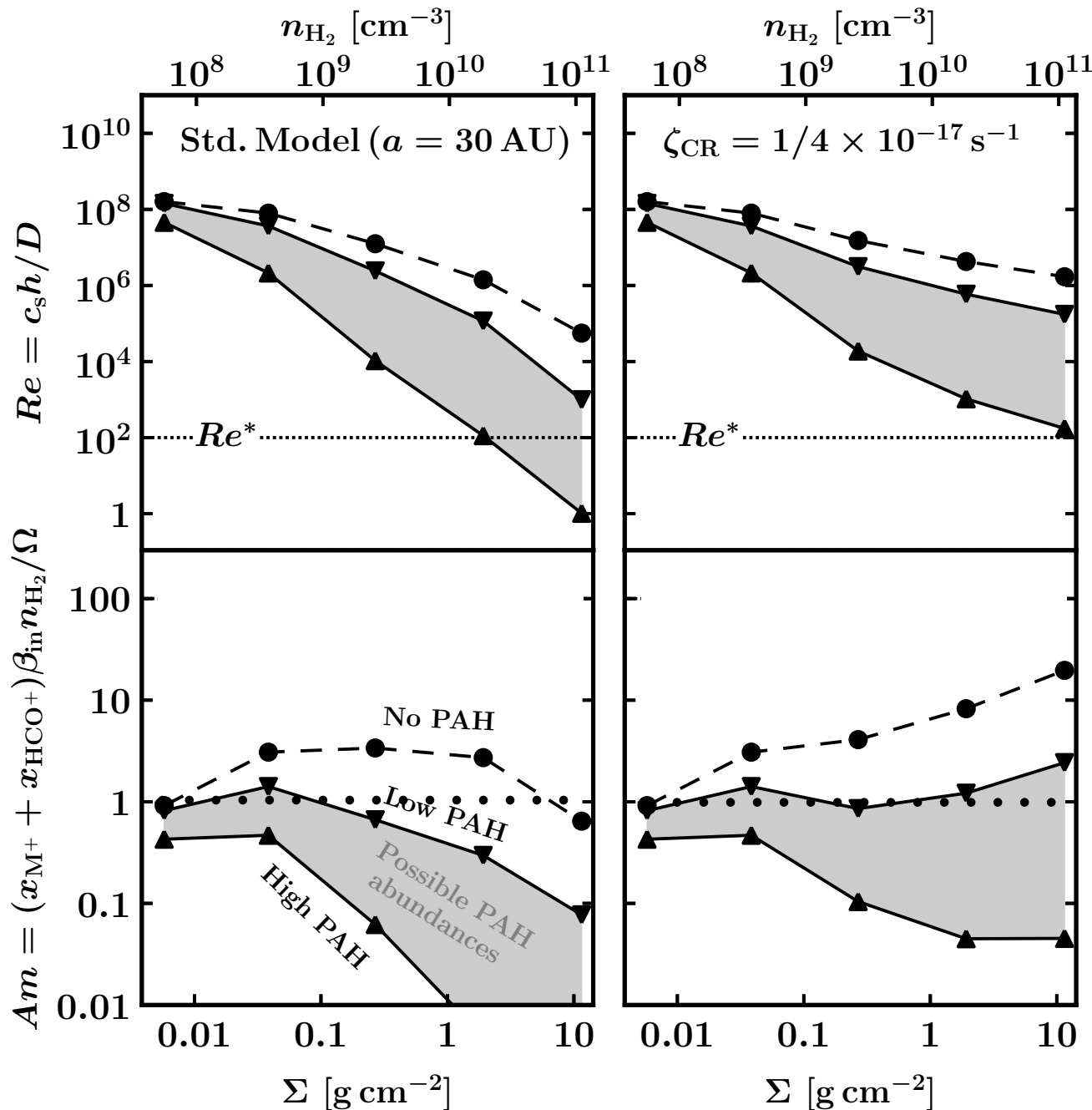
Imperfect  
clearing can  
lead to  
gapped disks  
(e.g. LkCa 15)

# X-ray ionized MRI-active surface layer



At 3 AU,  
 $Am \sim 1$  ( $\alpha \sim 10^{-3}$ )  
 $\Sigma_{\text{active}} \sim 1 \text{ g cm}^{-2}$

# X-ray ionized MRI-active surface layer



At 30 AU,

$$Am \sim 1 \quad (\alpha \sim 10^{-3})$$

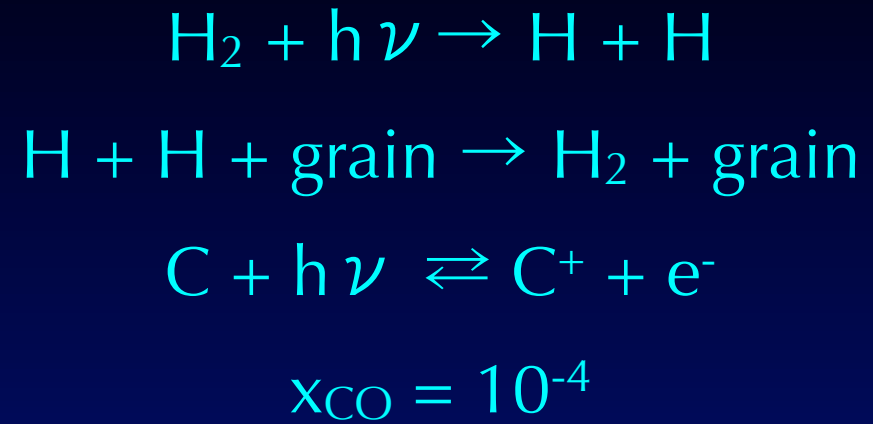
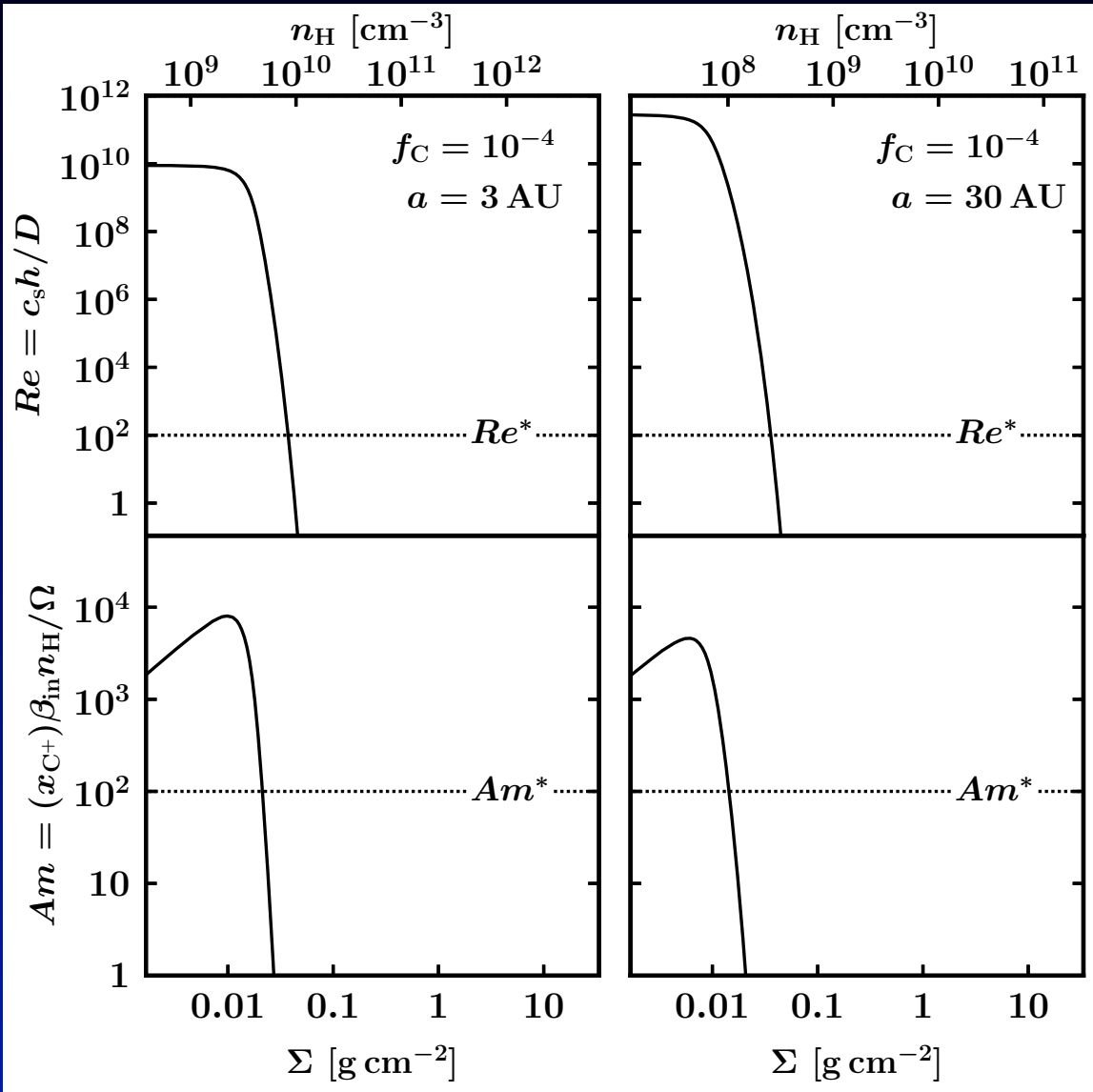
$$\Sigma_{\text{active}} \sim 0.1 \text{ g cm}^{-2}$$

if no cosmic rays

$$\Sigma_{\text{active}} \sim 10 \text{ g cm}^{-2}$$

if cosmic rays

# Far-UV (912-1100 Å) ionized MRI-active surface layer

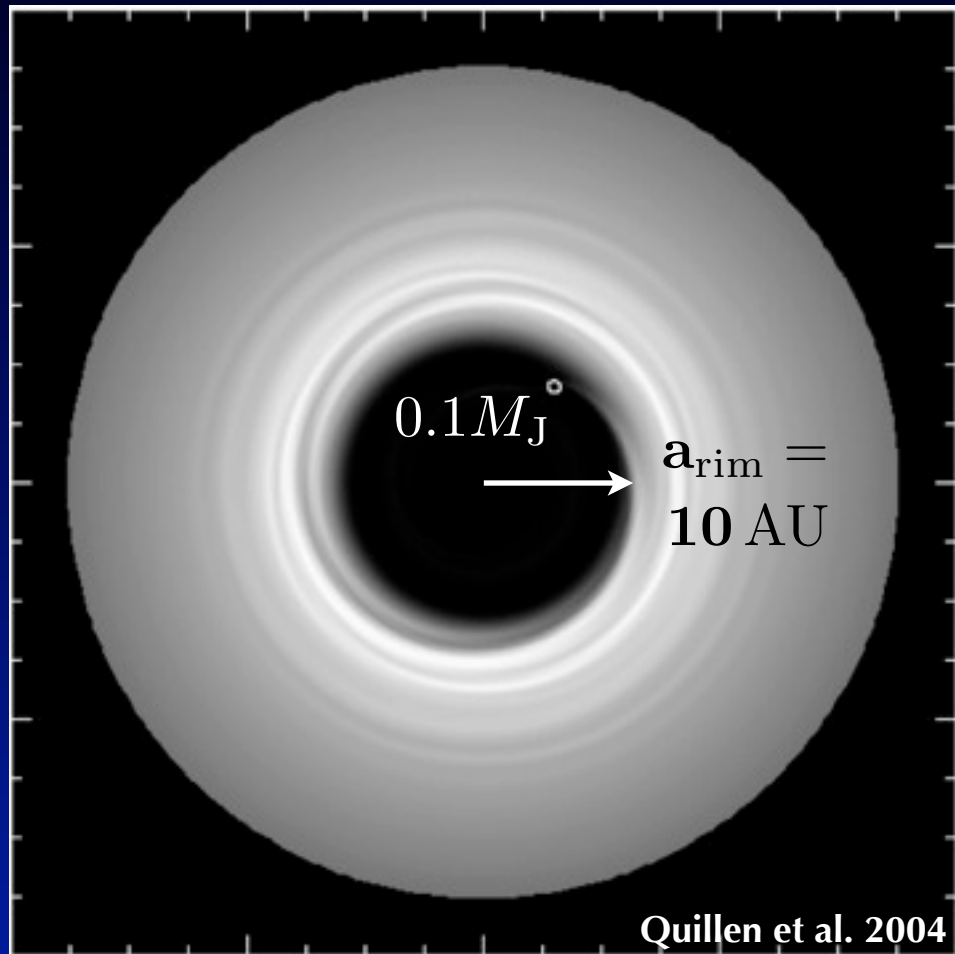


At 3-30 AU,

$$Am > 10^2 \quad (\alpha \sim 0.1)$$

$$\Sigma_{\text{active}} \sim 0.01 \text{ g cm}^{-2}$$

# Planet Clearing



$$\text{Initial } \Sigma_{\text{inner}} / \Sigma_{\text{outer}} = 0.01$$

Run duration = 100 orbits  
 $\ll$  Viscous time  $t_{\text{diff}} \sim 10000$  orbits

$$t_{\text{diff}} \sim a_{\text{rim}}^2 / \nu$$
$$\nu = \alpha c_s h$$

0.004 (assumed)

$\therefore$  Hole in simulation reflects assumed initial conditions

	$\Sigma_{\text{active}}$ (g/cm <sup>2</sup> )	$\alpha$	$T$ (K)	$\dot{M}$ ( $M_{\odot}$ /yr)
3 AU X-ray	1	$10^{-3}$	80	$10^{-11}$
3 AU Far-UV	0.01	0.1	300	$4 \times 10^{-11}$
30 AU X-ray+CR	0.1-10	$10^{-3}$	30	$10^{-11}$ - $10^{-9}$
30 AU Far-UV	0.01	0.1	300	$10^{-9}$



# Protoplanetary Disks

disk mass  $\sim 0.001$ - $0.1$  stellar mass

